

### Problem set #13

#### 1. Mirror Symmetry in 3 dimensions

Using a corresponding brane configuration compute the 3d mirror for the following theories. For each of these groups add  $n$  flavors in the fundamental representation and write down the corresponding quiver gauge theory both for the theory itself and for its mirror:

- a)  $U(1)$  with  $n$  flavors
- b)  $SU(2)$  with  $n$  flavors
- c)  $U(k)$  with  $n$  flavors
- d)  $Sp(k)$  with  $n$  flavors
- e)  $So(k)$  with  $n$  flavors
- f) Comment on the relation of the first two results to affine Dynkin diagrams.
- g) Using f) find a quiver for the moduli space of  $E_n$  instantons,  $n=6,7,8$ .
- h) What are the restrictions on  $n$  in each case?
- i) For each case compute the dimension of the moduli space on the Higgs branch and on the Coulomb branch and verify that there is a matching with the expectation that both theories are mirror to each other.

#### 2) Five dimensional fixed points and their low energy gauge theory limits

- a) Write down the  $(p,q)$  web representation for  $SU(2)$  gauge theory with  $n$  flavors for  $n=0,1,2$ .
- b) Find the corresponding parameters and moduli which contribute to the mass formula of the BPS states in the theory.
- c) Determine what are the  $W$ -boson, instanton and monopole for each theory.
- d) Find their corresponding mass and tension formulas in terms of the underlying parameters and moduli found in b)

#### 3) Continuation past infinite coupling

- a) Consider a 5 dimensional (8 supercharges)  $SU(n)$  gauge theory with  $k$  flavors in the fundamental representation. Write down the set of parameters and moduli of the gauge theory.
- b) Find the continuation past infinite coupling for these theories.
- c) For the case  $n=4, k=0$  write down a map between the parameters and moduli in both theories
- d) Find how many different, in-equivalent, theories are there for the case  $n=4, k=0$ .