

# 2.76/2.760 Multiscale Systems Design & Manufacturing

Fall 2004

## Piezoelectricity-2

# Spontaneous polarization

$$\Delta \vec{P} = \vec{P}(\text{polar}) - \vec{P}(\text{nonpolar}) / a^2 c$$

: Polarization per unit cell volume

● Ba<sup>2+</sup>

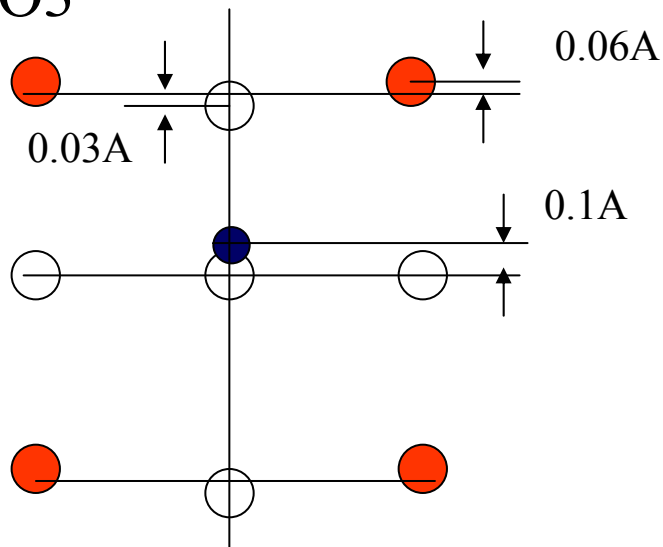
○ O<sup>2-</sup>

● Ti<sup>4+</sup>



Figure by MIT OCW.

BaTiO<sub>3</sub>



0.06A

0.03A

0.1A

Spontaneous Polarization = 0.145 C/ m<sup>2</sup>

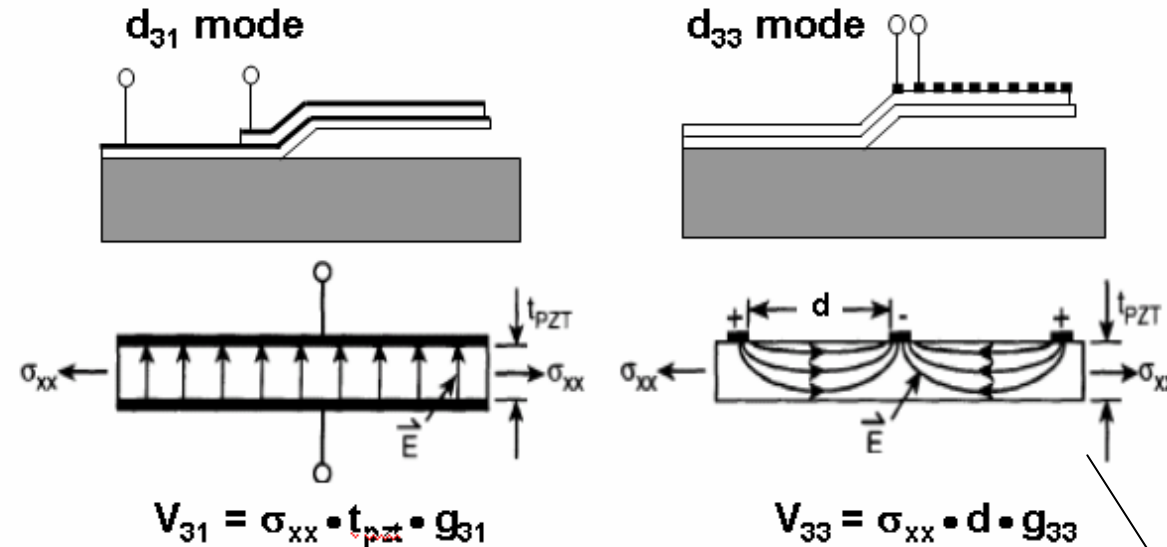
HW1: Calculate the magnitude of spontaneous Polarization.  $a=3.992 \text{ \AA}$ ,  $c=4.036a$   
 $1e=1.602 \times 10^{-19} \text{ C}$

$$\begin{aligned} \text{Dipole moment} &= \Sigma \text{ charge} \times \text{position shift} \\ &= 8(2e/8)(0.06 \times 10^{-10} \text{ m}) + 4e(0.1 \times 10^{-10} \text{ m}) \\ &\quad + 2(-2e/2)(-0.03 \times 10^{-10} \text{ m}) \\ &= 0.9292 \times 10^{-29} \text{ C m} \end{aligned}$$

$$\text{Volume} = a \times a \times c = 64.3 \times 10^{-30} \text{ m}^3$$

# $d_{31}$ vs $d_{33}$

HW2: Compare generated voltages  $V_{31}$  (from  $d_{31}$  mode),  $V_{33}$  ( $d_{33}$  mode). Both have same cantilever dimension, but different electrodes.

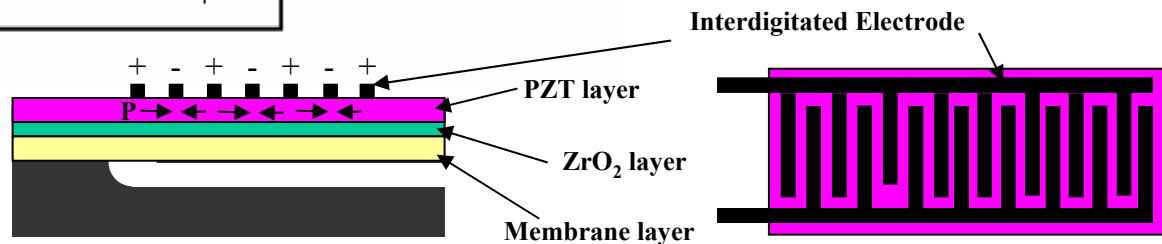


$$V_{33} = \frac{2d}{t_{pzt}} \cdot V_{31} \approx 20 \cdot V_{31}$$

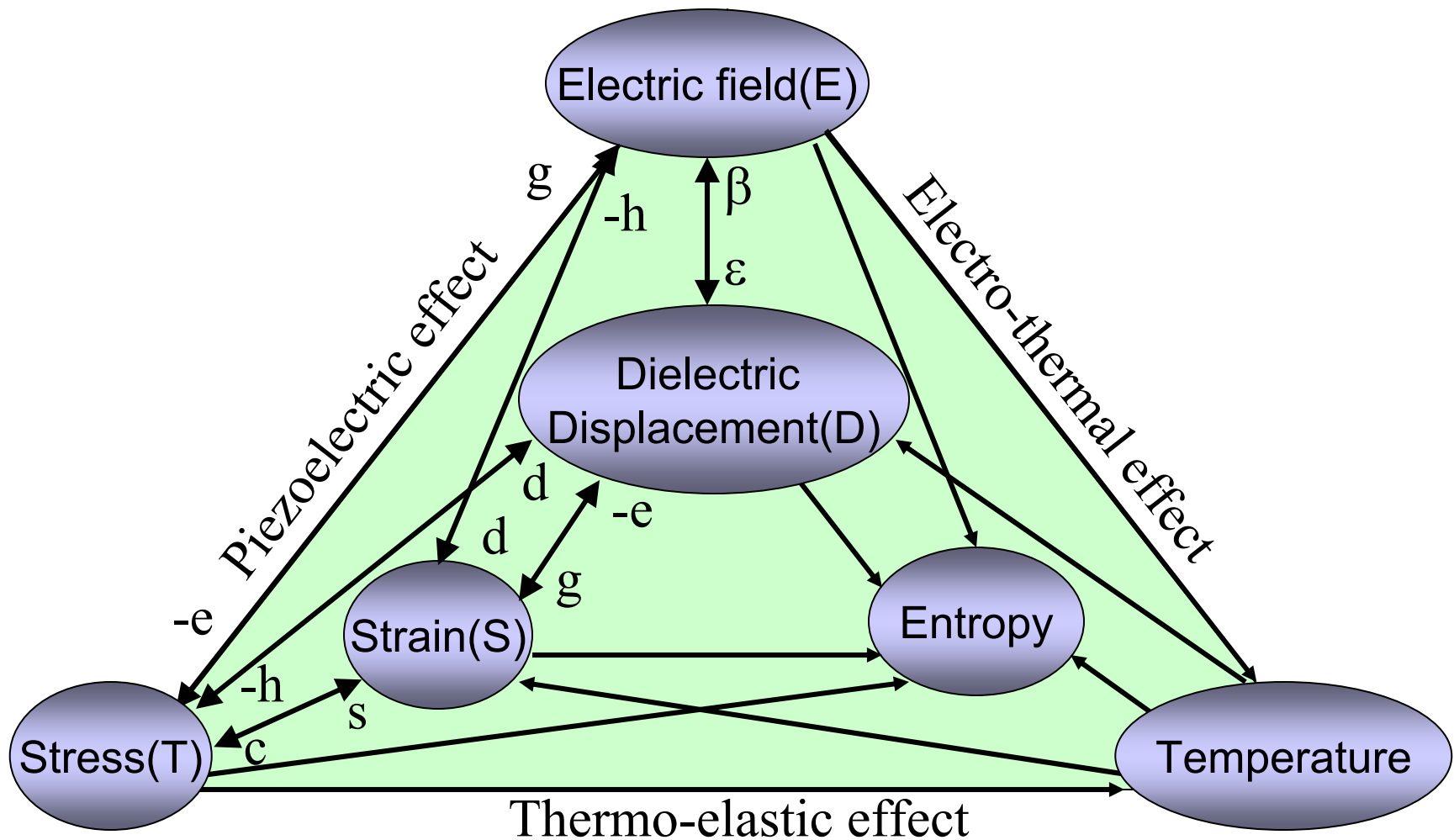
(if  $g_{33} > 2g_{31}$ ,  $d \approx 10 t_{pzt}$ )

Assume,  $g_{33} = 2g_{31}$   
 $t_{pzt} = 0.5 \mu$   
 $d = 5 \mu$   
 length =  $100 \mu$ , width =  $50 \mu$   
 Young's modulus of the beam = 65 Gpa, **max strain = 0.1%**

$d_{33} = 200 \text{ pC/n}$   
 $K = 1000$



# Principles of piezoelectric



# Piezoelectricity

Direct effect

$$D = Q/A = dT$$

$$E = -gT$$

Converse effect

$$S = dE$$

$$g = d/\epsilon = d/K\epsilon_0$$

- D: dielectric displacement, electric flux density/unit area
- T: stress, S: strain, E: electric field
- d: Piezoelectric constant, [Coulomb/Newton]

# Piezoelectric Charge Constants

Electrical energy

Actuator

Mechanical energy

**Longitudinal ( $d_{33}$ )**

Diagram removed for copyright reasons.  
Source: Piezo Systems, Inc.  
"Introduction to Piezo Transducers."  
<http://www.piezo.com/benedu.html>

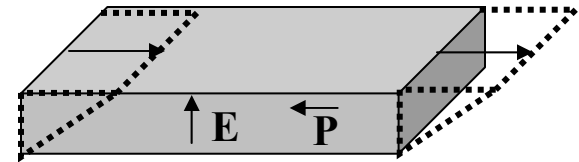
$$\Delta T/T = d_{33} \cdot E$$

**Transverse ( $d_{31}$ )**

Diagram removed for copyright reasons.  
Source: Piezo Systems, Inc.  
"Introduction to Piezo Transducers."  
<http://www.piezo.com/benedu.html>

$$\Delta L/L = d_{31} \cdot E$$

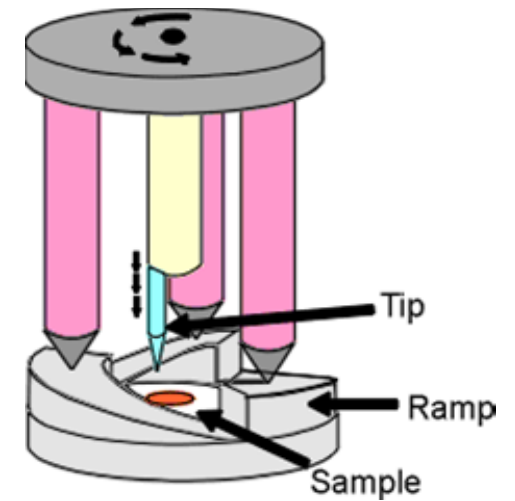
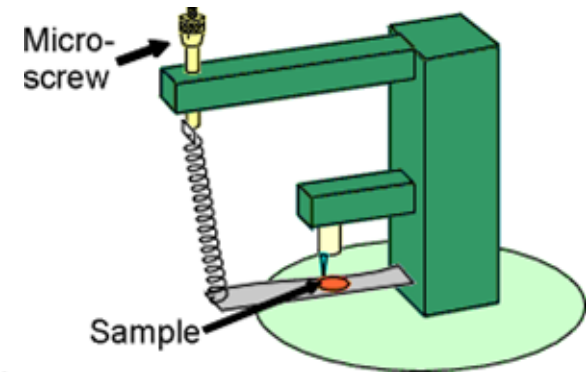
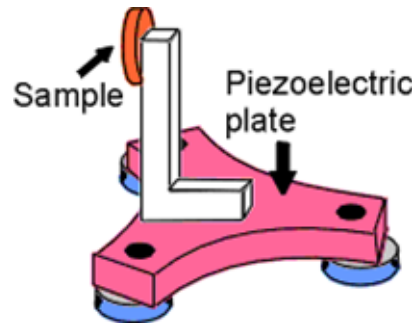
**Shear ( $d_{15}$ )**



$$\text{Shear strain} = d_{15} E$$

# Coarse Positioning

- Screw
- Louse
- Beetle



Courtesy of Friedrich-Alexander University. Used with permission.  
Source: "Scanning Tunneling Microscopy"  
<http://www.fkp.uni-erlangen.de/methoden/stmtutor/stmtech.html>

# STM tip scanning

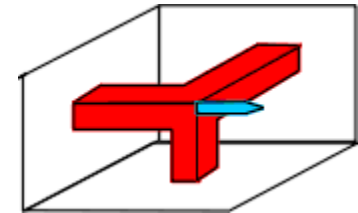
- Tripod

$$\Delta x = d_{31} V \frac{L}{h} \quad \frac{\Delta x}{V} = d_{31} \frac{L}{h}$$

For L=20mm, h=2mm, PZT-5H

$$\frac{\Delta x}{V} = ?$$

Resonant frequency=?



Courtesy of Friedrich-Alexander University. Used with permission.  
Source: "Scanning Tunneling Microscopy"

<http://www.fkp.uni-erlangen.de/methoden/stmtutor/stmtech.html>

PZT-5H

d<sub>31</sub>: -2.74 Angstrom/V

d<sub>33</sub>: 5.93 A/V

E: 6.1 10<sup>10</sup>N/m<sup>2</sup>

T<sub>c</sub>: 195 C

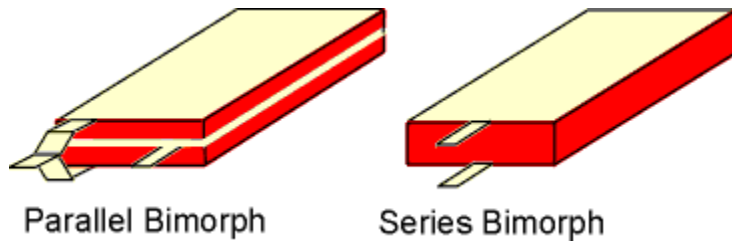
Q: 65

ρ: 7.5g/cm<sup>3</sup>

C: 2.8 km/sec

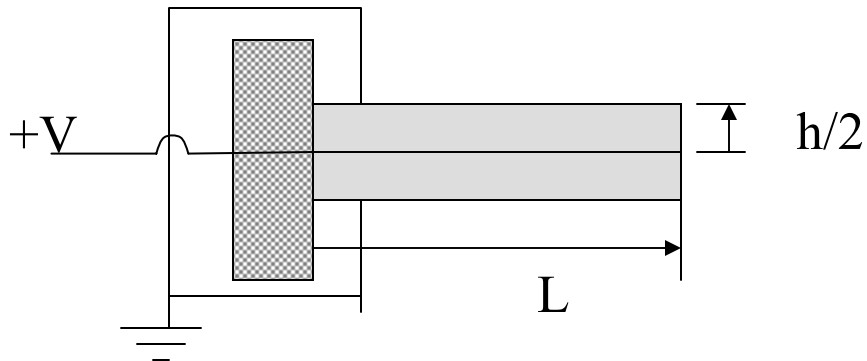


# Bimorph bender



Courtesy of Friedrich-Alexander University. Used with permission.

Source: "Scanning Tunneling Microscopy" <http://www.fkp.uni-erlangen.de/methoden/stmtutor/stmtech.html>



$$\sigma_1 = \pm E d_{31} V \frac{1}{h/2}$$

$$\sigma(z) = \sigma_1 - \alpha z$$

$$M = 0 = \int z \sigma(z) dz$$

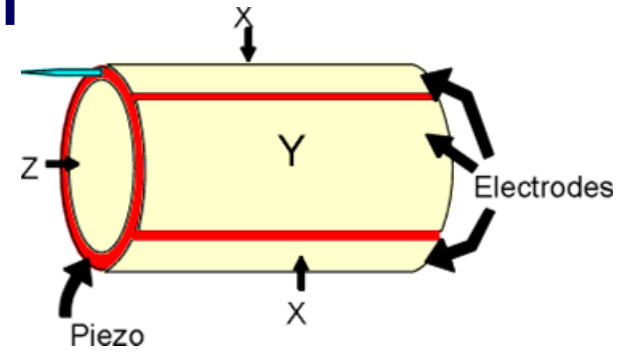
$$\alpha = \frac{3\sigma_1}{h}$$

$$\text{radius: } \rho = \frac{h^2}{6d_{31}V}$$

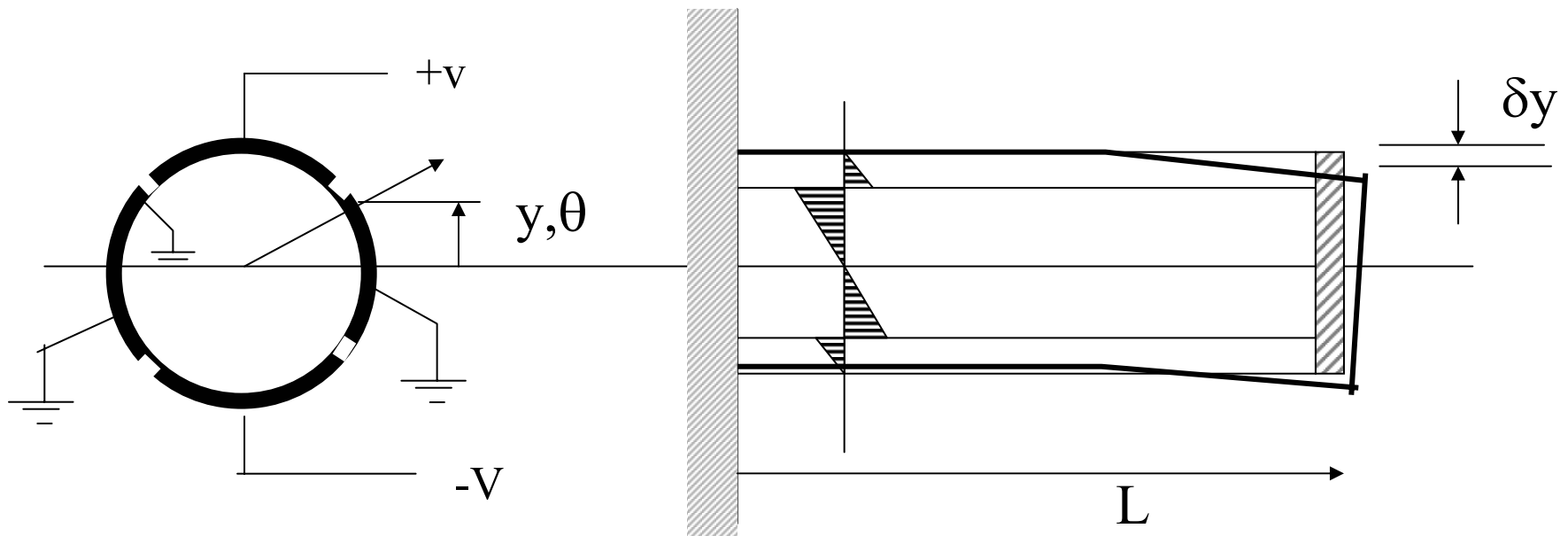
$$\Delta z = 3d_{31}V \frac{L^2}{h^2}$$

# Tube scanner

- Piezo Tube with  $1/4$  electrodes



Courtesy of Friedrich-Alexander University. Used with permission.  
Source: "Scanning Tunneling Microscopy" <http://www.fkp.uni-erlangen.de/methoden/stmtutor/stmtech.html>



# Tube scanner, deflection

Curvature

$$R = \frac{\pi D h}{4\sqrt{2}d_{31}V}$$
$$\delta y = \frac{2\sqrt{2}d_{31}VL^2}{\pi D h}$$

Resonant frequency 40KHz (z), 8 KHz(x,y),  
For a tube of 12.7mm L, 6.35 mm diameter, 0.51mm thick

# Design of a Z-axis scanner

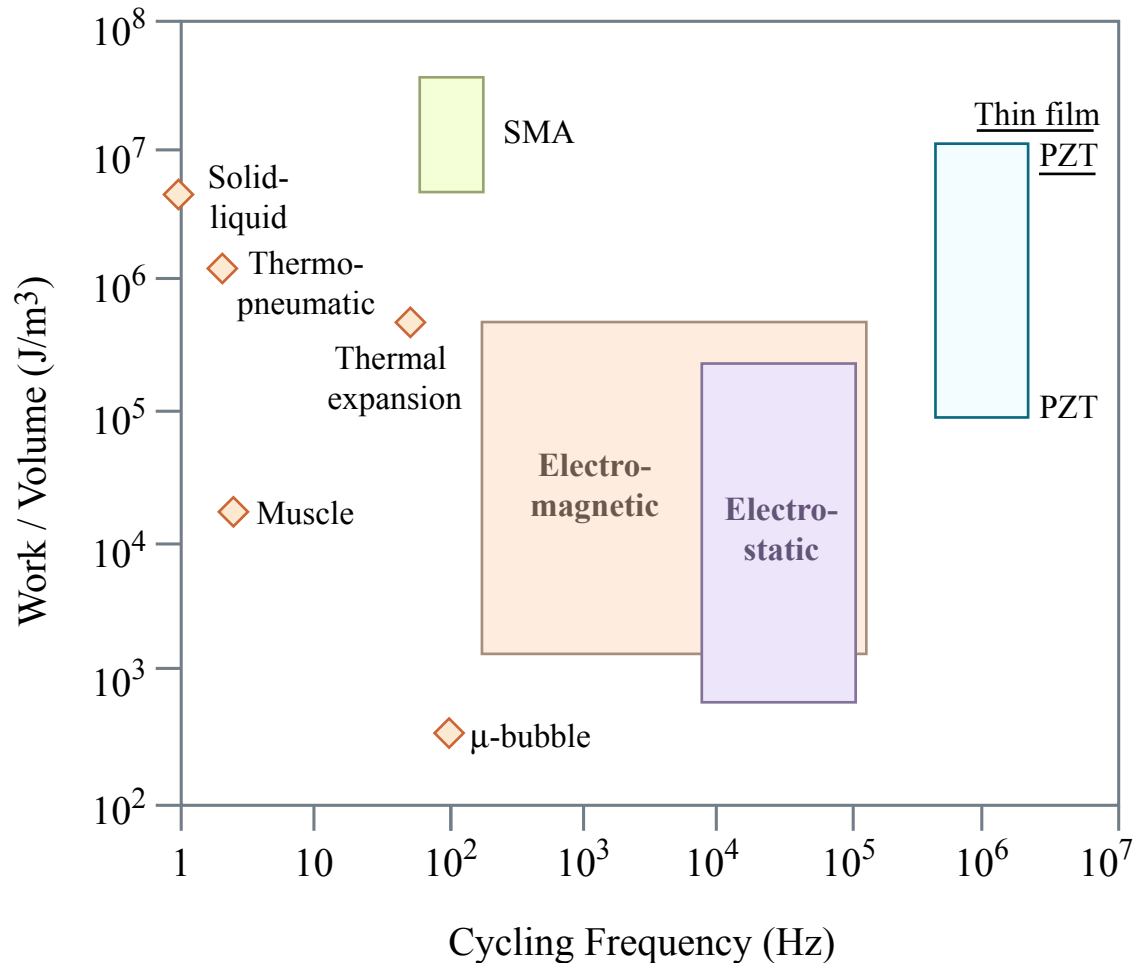
Component schematic removed for copyright reasons.

Physik Instrumente Z-positioner P-882.10,

in [http://www.pi-usa.us/pdf/2004\\_PICatLowRes\\_www.pdf](http://www.pi-usa.us/pdf/2004_PICatLowRes_www.pdf), page 1-45.

Ordering Number*	Dimensions A x B x L [mm]	Nominal Displacement [ $\mu\text{m}$ @ 100 V] ( $\pm 10\%$ )	Max. Displacement [ $\mu\text{m}$ @ 120 V] ( $\pm 10\%$ )	Blocking Force [N @ 120 V]	Stiffness [N/ $\mu\text{m}$ ]	Electrical Capacitance [ $\mu\text{F}$ ] ( $\pm 20\%$ )	Resonant Frequency [kHz]
P-882.10	2 x 3 x 9	7	9	215	26	0.13	135

# Case 1: Piezoelectric micro-actuators

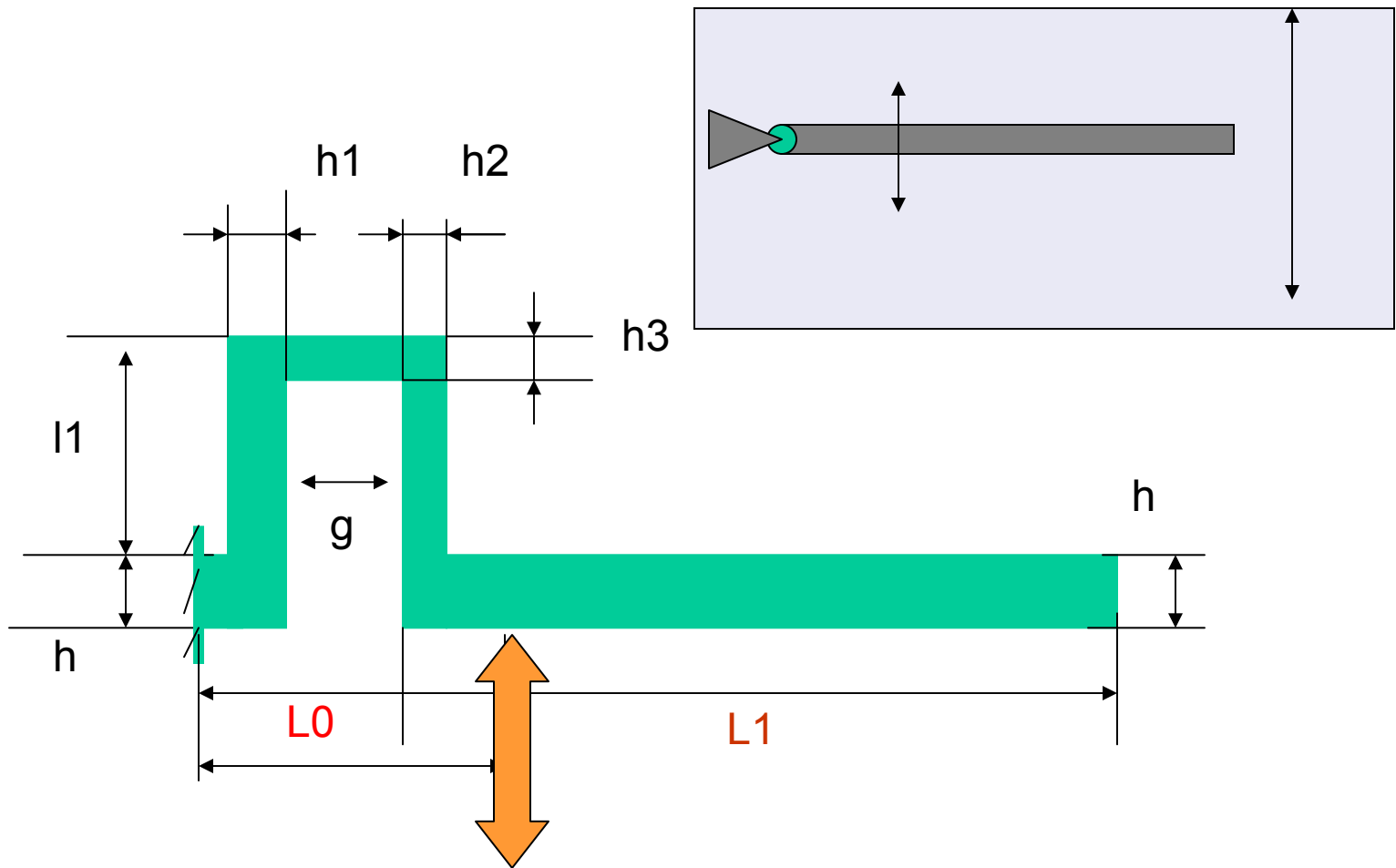


## Positives

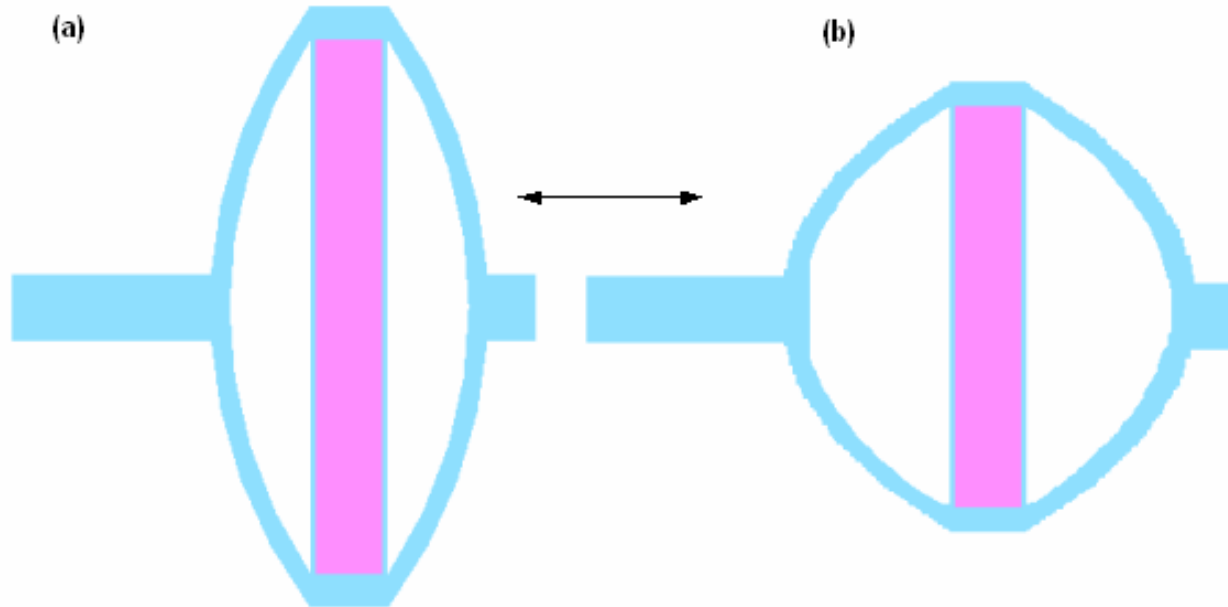
1. Low power and voltage for thin films
2. High force
3. Compact

Modified from P. Kruevitch et al, "Thin Film Shape Memory Alloy Microactuators," JMEMS Vol. 5, No. 4. 1996 pp 270-282.

# Leveraged Amplification

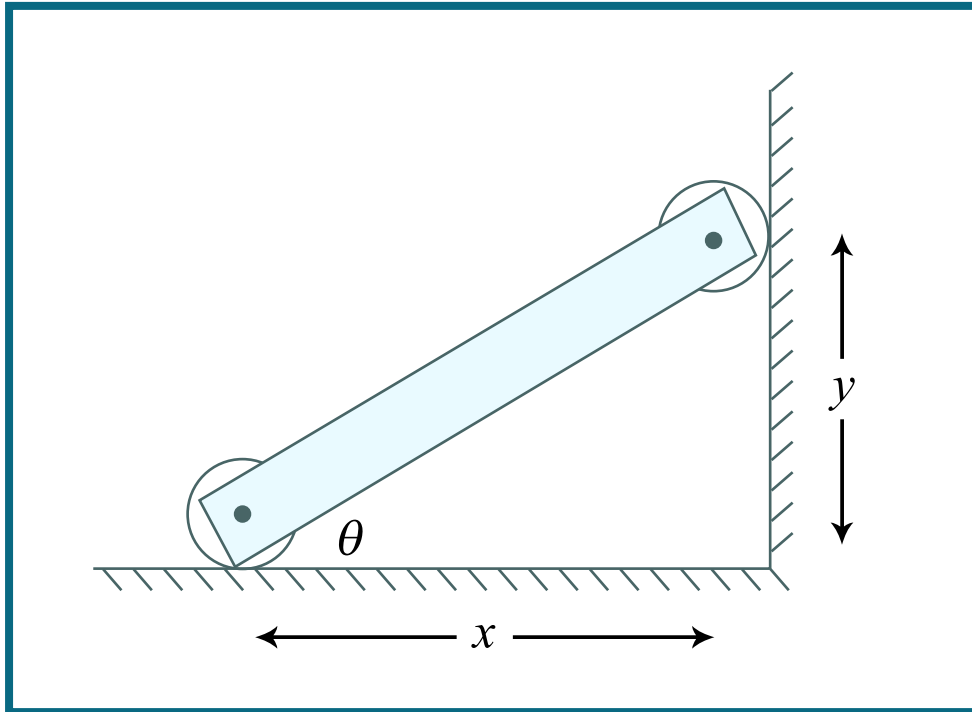


# Bow Strain Amplifier



US Patent pending, N. Conway, S. Kim

# Amplification depends on 2 factors



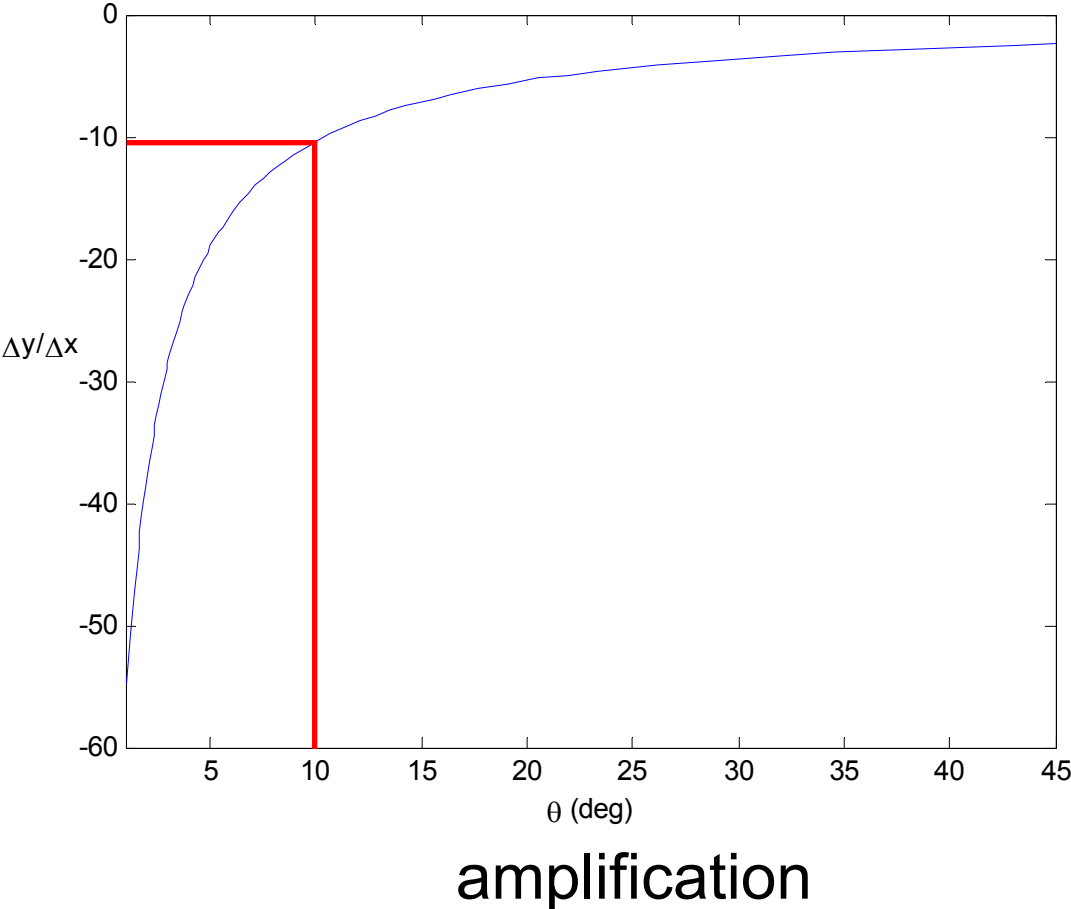
$\theta_0$  = initial angle

Figure by MIT OCW.

$$\frac{\Delta y}{\Delta x} = \frac{\sin \theta - \sin \theta_0}{\cos \theta - \cos \theta_0} = -\theta \cot \left( \frac{1}{2} (\theta + \theta_0) \right)$$



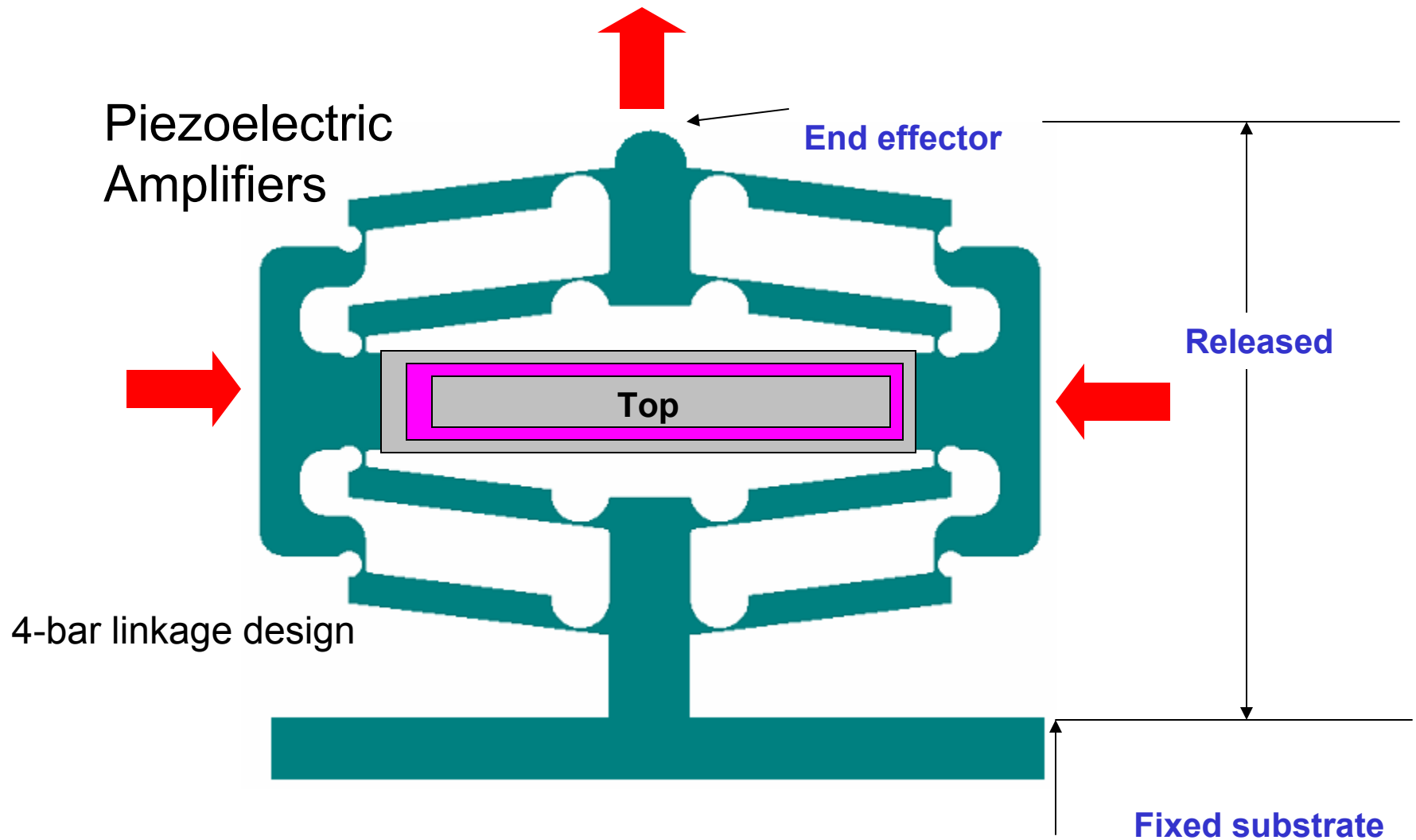
# Small angles yield enormous amplification



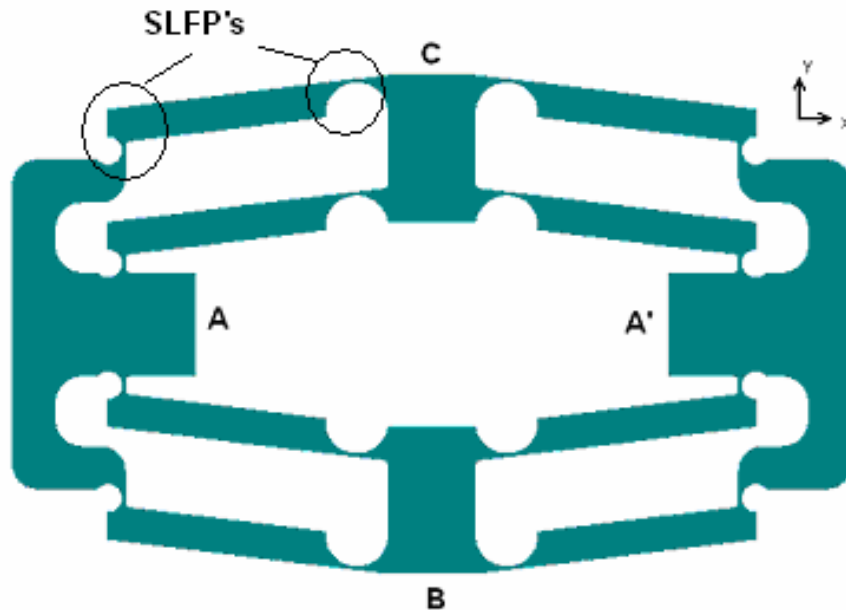
$$\theta_0 = 1^\circ$$

# MIT Bow-actuator

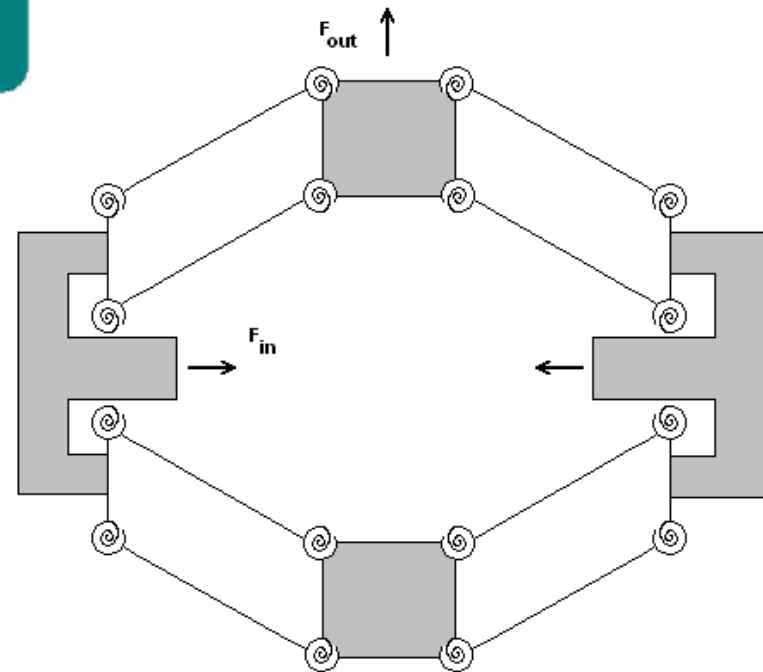
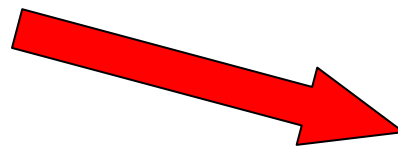
Nick Conway, MS 2003



Flexural pivots enable a parallel guiding linkage in a high aspect ratio structure.

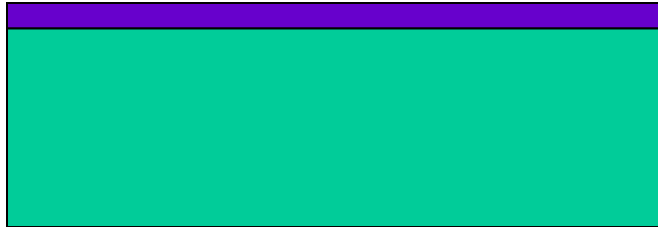


$$k_{\theta} \approx \frac{YI}{L}$$



# Process Flow 1- 4 mask process

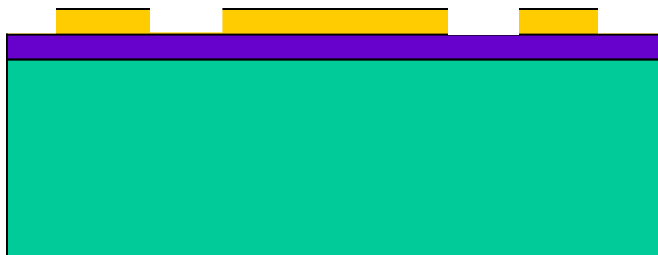
1



Deposit oxide ( $\text{SiO}_2$ )  
layer on Si substrate

---

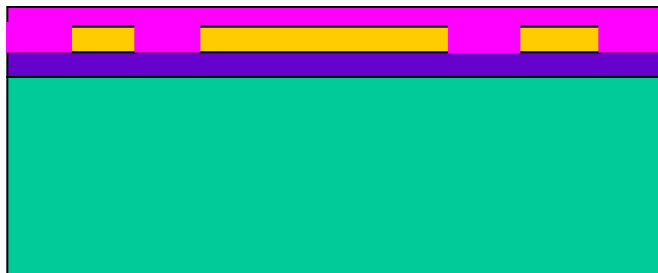
2



Deposit and pattern  
Pt/Ti bottom electrode  
layer (#1)

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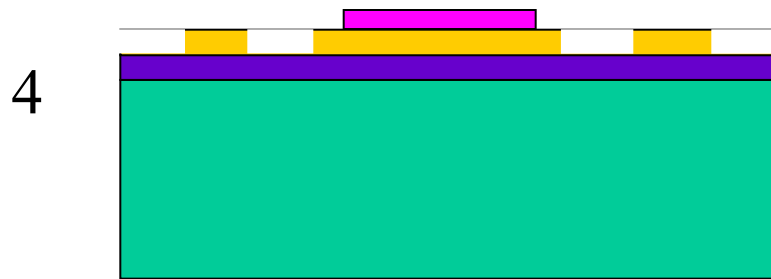
3



Spin-on PZT

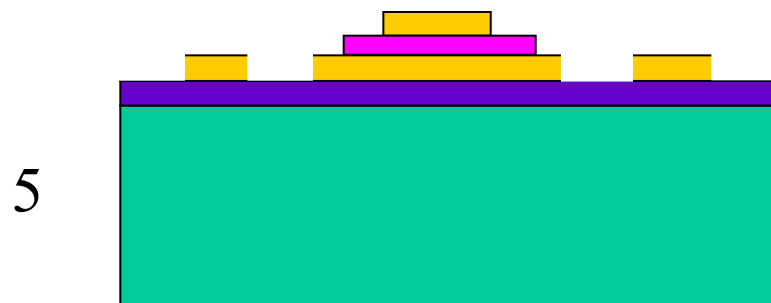
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# Process Flow 2



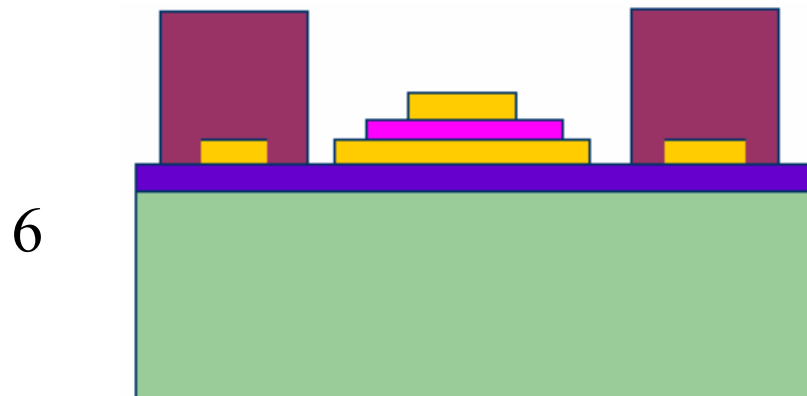
Pattern then anneal  
PZT (#2)

---



Deposit top electrode  
(platinum) (#3)

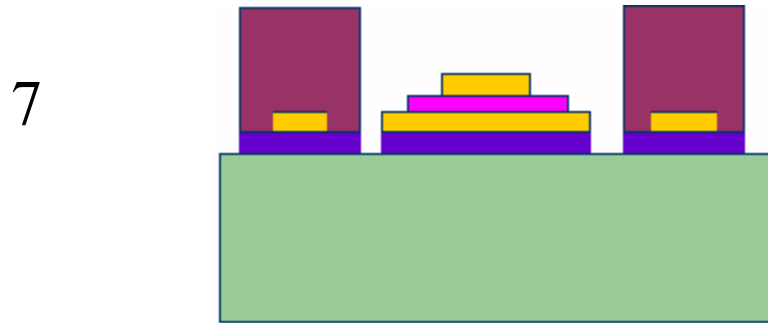
---



Spin-on SU-8 (30  $\mu\text{m}$ ) and  
cure, expose, and develop  
(#4)

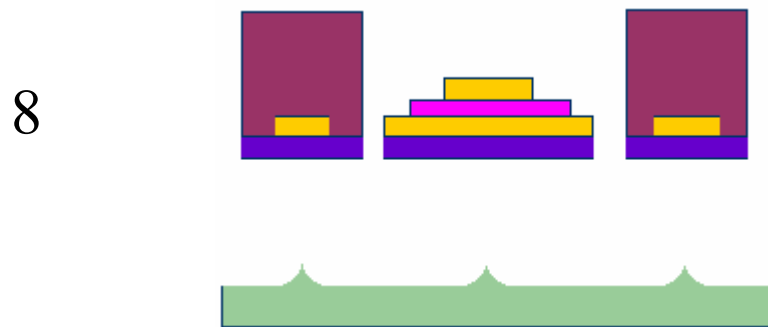
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# Process Flow 3



RIE oxide

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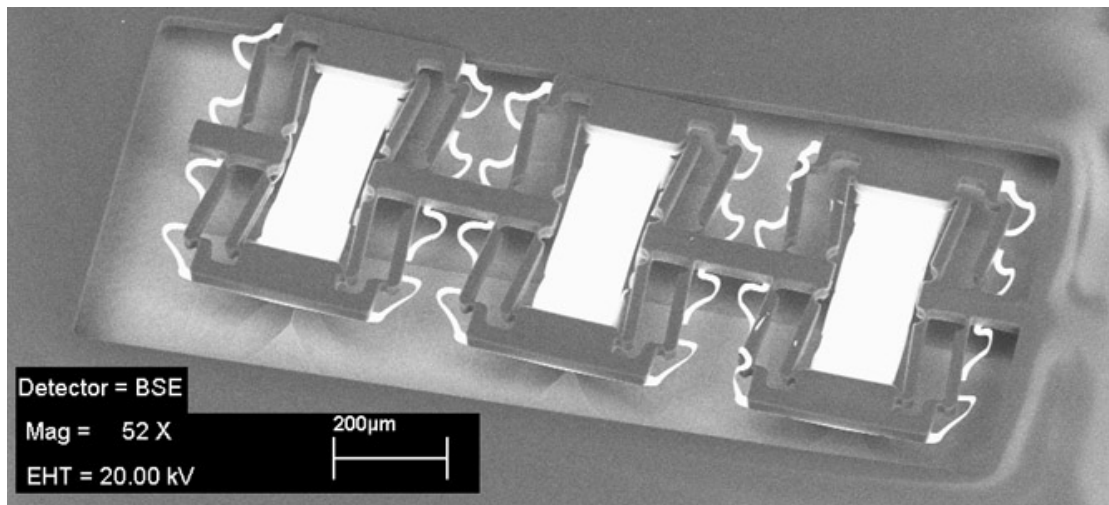
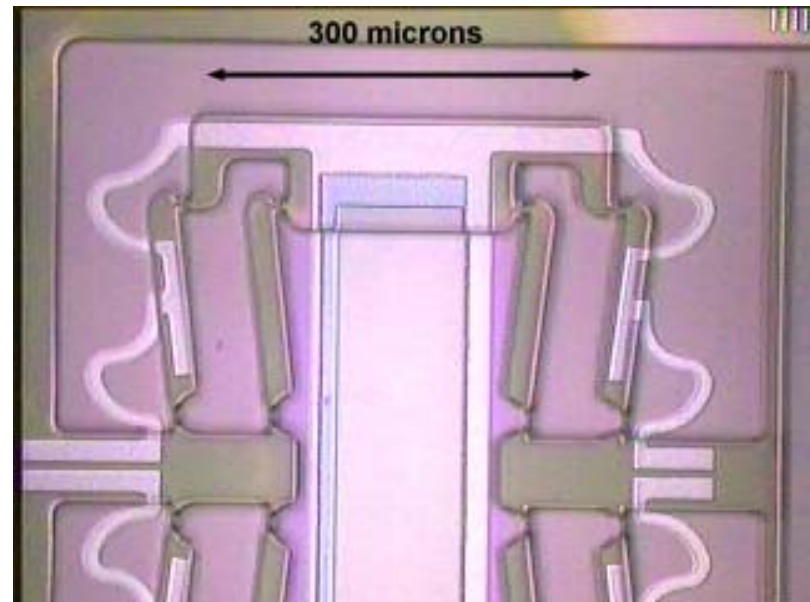


XeF<sub>2</sub> etch away Si to  
release actuator

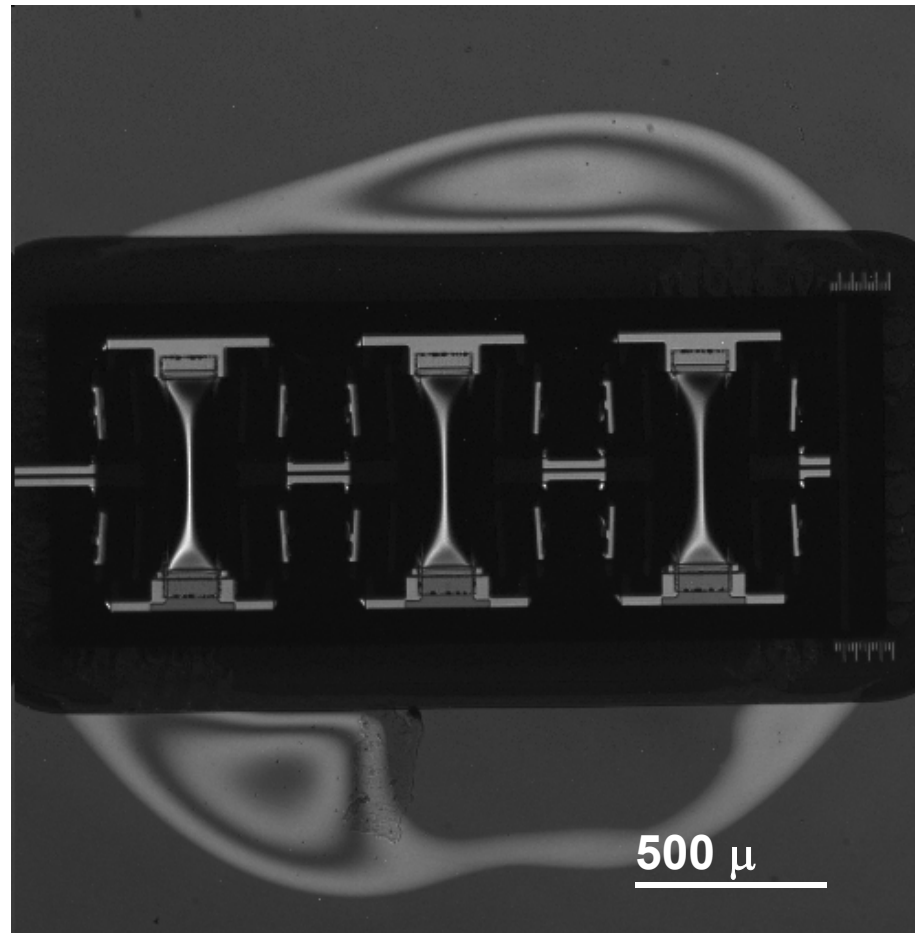
---

# Finished

Note: SU-8 non-conducting.



# MEMS-Strain-Amplifier

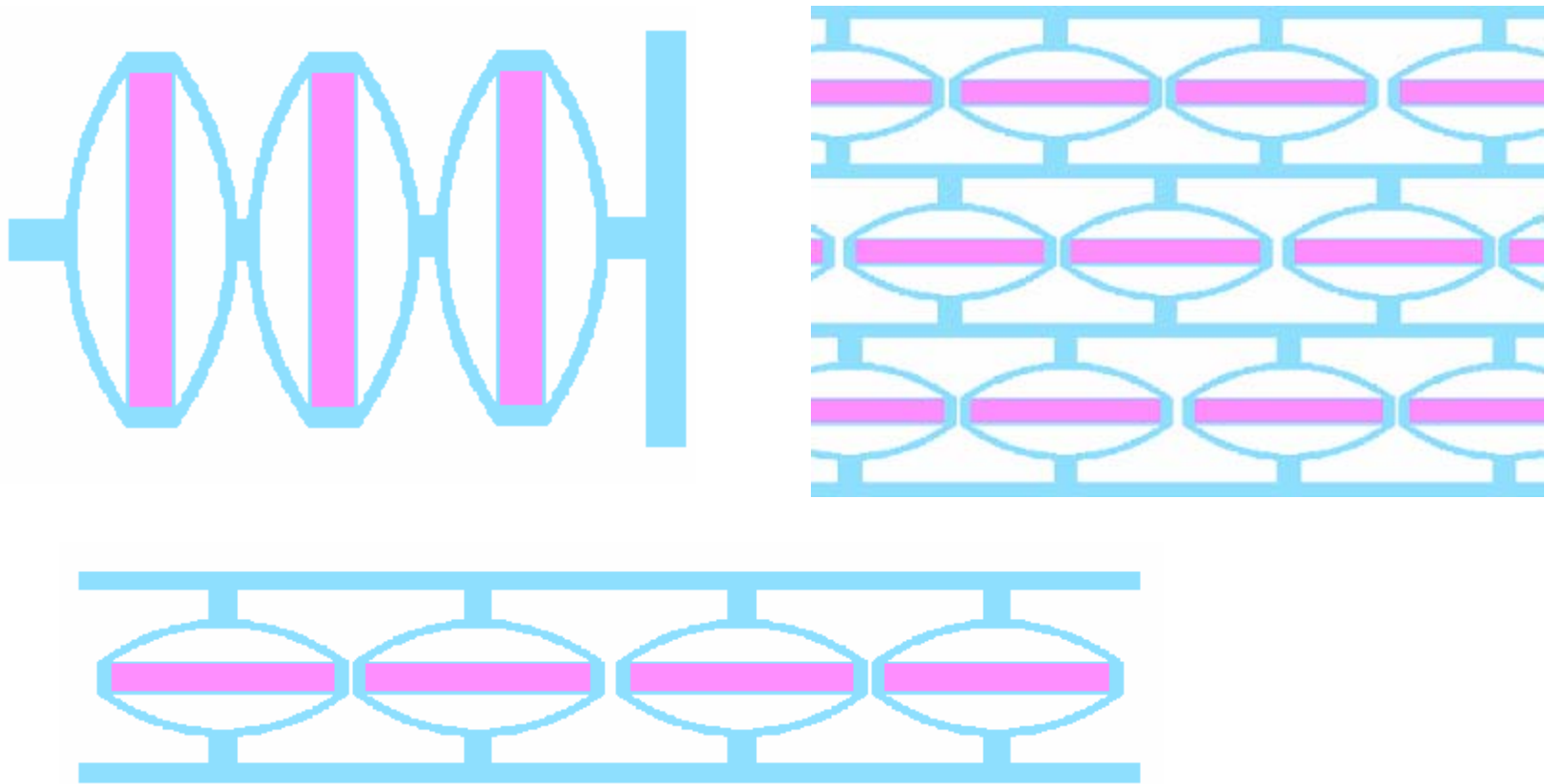


Nick Conway, Micronanosystems Laboratory, MIT

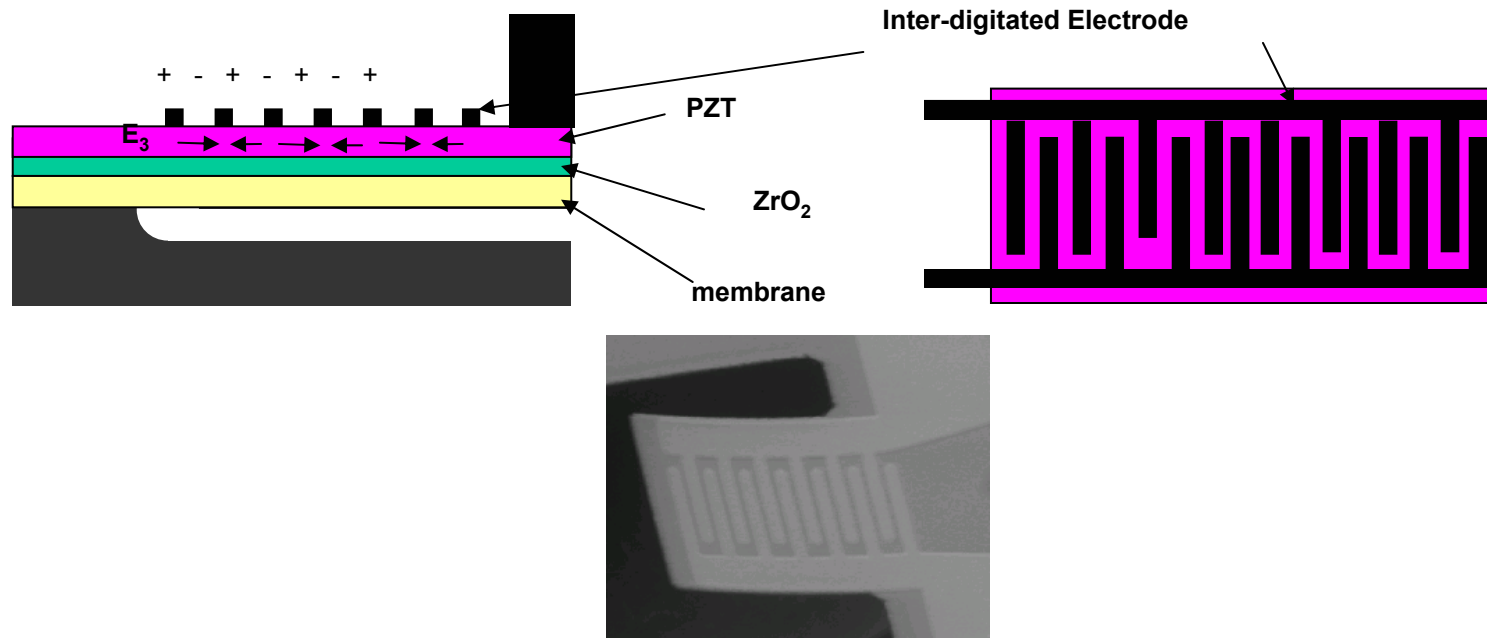
Sang-Gook Kim, MIT



# Arrayed configurations – Cellular analog digital actuation



# Case: Piezoelectric Micro Power Generator



**MIT Media Lab, Shoe Power**



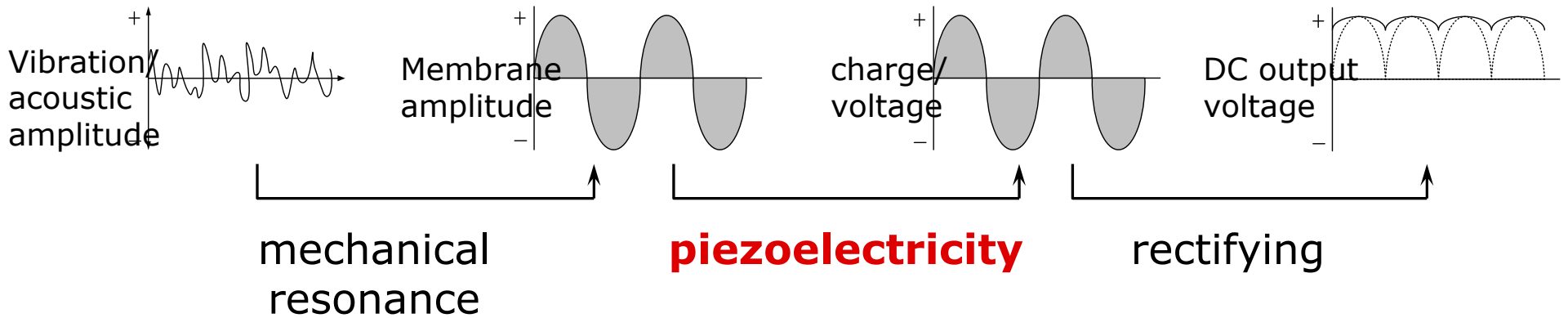
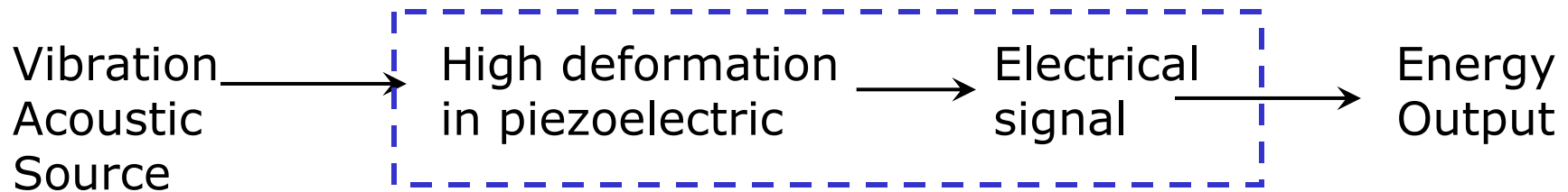
**MIT EECS, Chandrakasan  
Energy Amplifier**

# Comparison of Energy Scavenging

<b>Energy Source</b>	<b>Power Density for 10 Years</b>
Solar (outdoor)	15,000 $\mu\text{W}/\text{cm}^3$
Solar (indoor)	6 $\mu\text{W}/\text{cm}^3$
Vibrations (piezoelectric)	250 $\mu\text{W}/\text{cm}^3$
Vibrations (electrostatic)	50 $\mu\text{W}/\text{cm}^3$
Acoustic noise	0.003 $\mu\text{W}/\text{cm}^3$ (at 75 dB)
Temperature gradient	15 $\mu\text{W}/\text{cm}^3$ (at 10 °C gradient)
Batteries (non-rechargeable)	3.5 $\mu\text{W}/\text{cm}^3$ (45 $\mu\text{W}/\text{cm}^3$ one year life)
Batteries (rechargeable)	0 $\mu\text{W}/\text{cm}^3$ (7 $\mu\text{W}/\text{cm}^3$ one year life)
Hydrocarbon fuel (micro heat engine)	33 $\mu\text{W}/\text{cm}^3$ (330 $\mu\text{W}/\text{cm}^3$ one year life)
Fuel cells (methanol)	28 $\mu\text{W}/\text{cm}^3$ (280 $\mu\text{W}/\text{cm}^3$ one year life)

*Shad Roundy, Paul K. Wright, Jan Rabaey, Computer Communications xx(2003) 1-14*

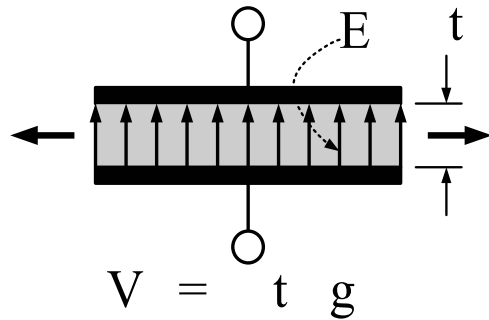
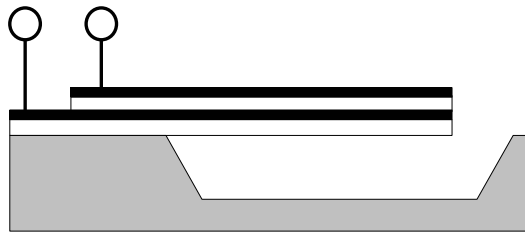
# Energy Harvesting Concept with Piezoelectricity



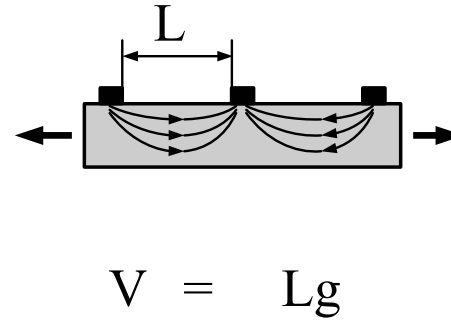
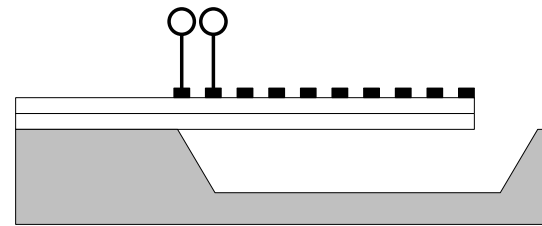
- Energy conversion efficiency ( $\eta_p$ )  
 $\eta_p = \text{generated energy} / \text{input energy}$   
 $\approx 65 \text{ to } 78 \%$  → JMM, 14, 717
- No voltage source needed
- Open circuit voltage: 3~15V

# Piezoelectrics

d mode



d mode



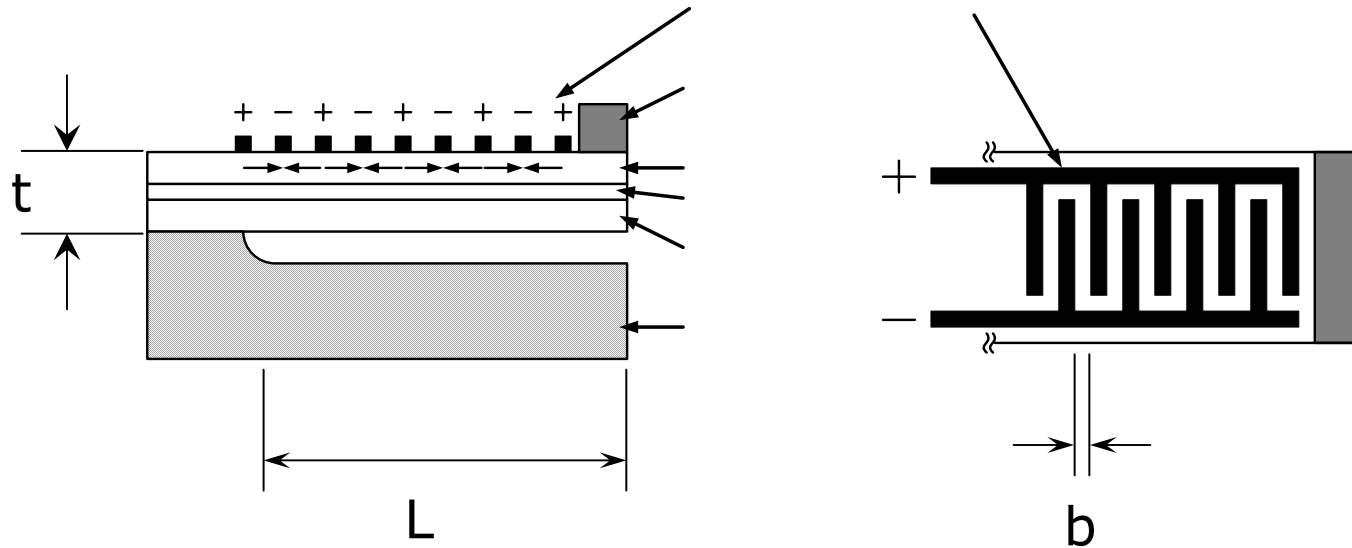
$$V_{33} = 2L / t_{pzt} \cdot V_{31} \cong 20 \cdot V_{31} \cong 3 V$$

$$g_{33} > 2g_{31}$$

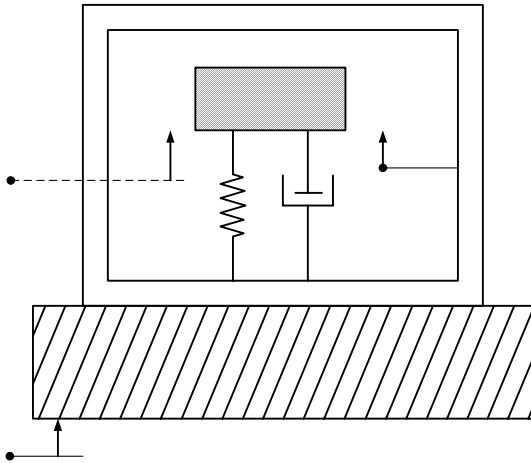
$$L \sim 10t_{pzt}$$

# Device Design

- High strain: cantilever beam, proof mass
- High open-circuit voltage:  
 $d_{33}$  interdigitated electrodes



# Device Modeling



## Governing equation for seismic excitation

$$m\ddot{z}_o = -b_m\dot{z}_o - kz_o + (EMC) - m\ddot{z}_i$$



$$m\ddot{\delta} + b_m\dot{\delta} + k\delta - k\frac{d_{33}V_L}{b} = \frac{3t}{4L^2}m\ddot{z}_i$$

## Open Circuit Voltage of PMPG

$$V_s = bE = -\frac{bd_{33}Y}{\varepsilon(1 - k_{33}^2)}\delta$$

Y: Young's modulus

$\delta$ : strain

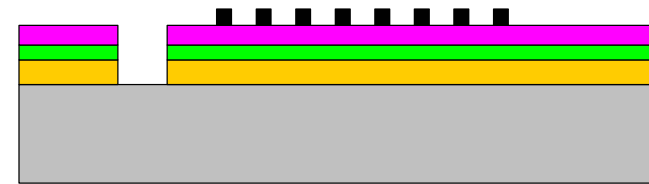
d: piezoelectric coeff.

$k_{33}$ : coupling constant

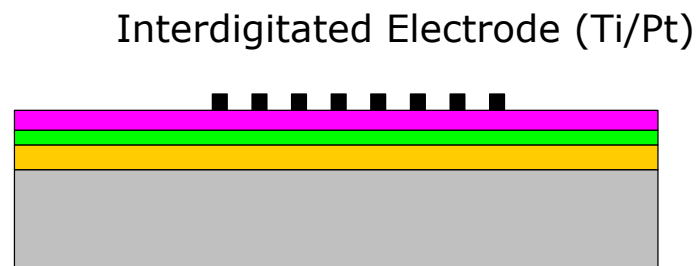
# Device Fabrication



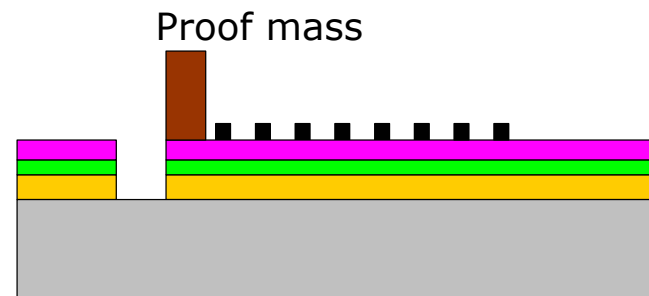
(a) Films deposition (CVD, spinning)






(c) Films patterning (RIE)



(b) Top electrode deposition (e-beam)  
and then lift-off

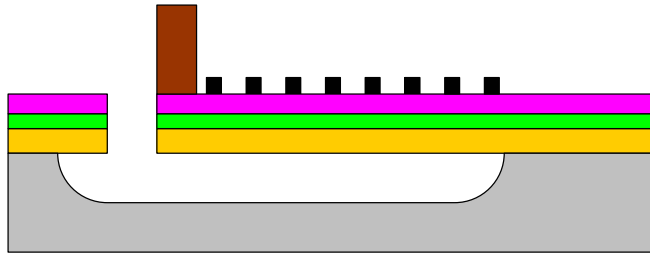


(d) Proof mass (SU-8, spinning)

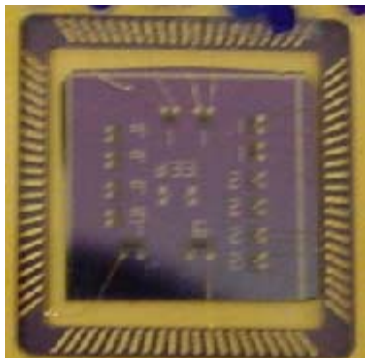
PZT ( $\text{Pb}(\text{Zr},\text{Ti})\text{O}_3$ )   
ZrO<sub>2</sub>   
Membrane 



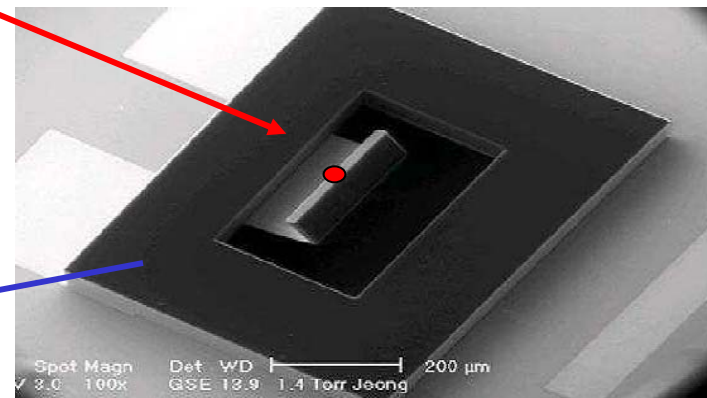
# Device Fabrication (II)



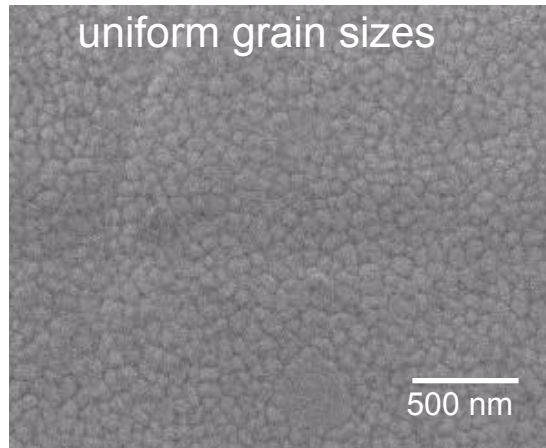
(e) Cantilever release ( $\text{XeF}_2$  etcher)



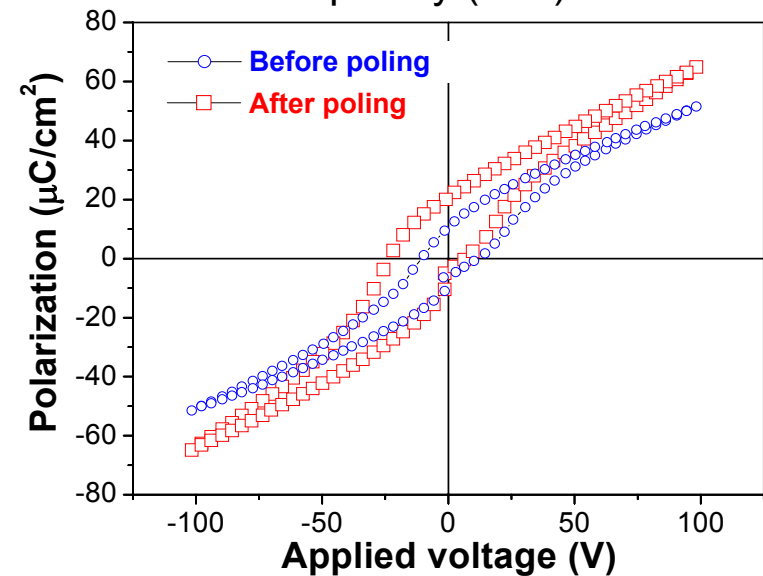
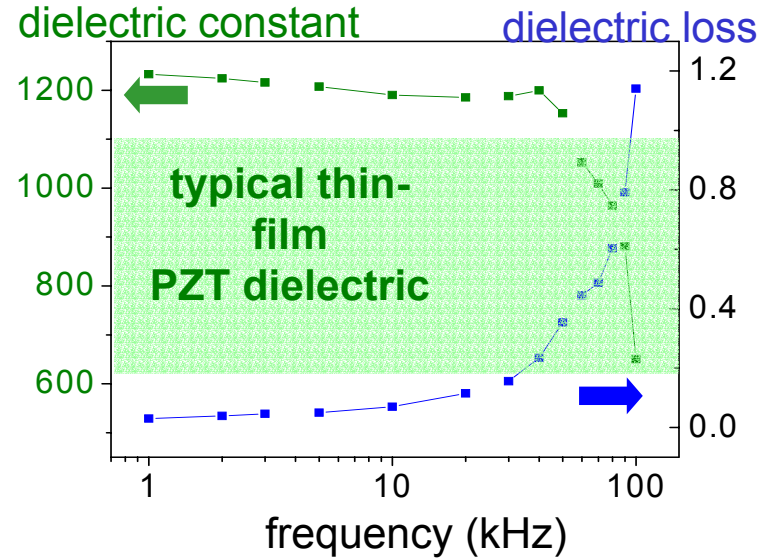
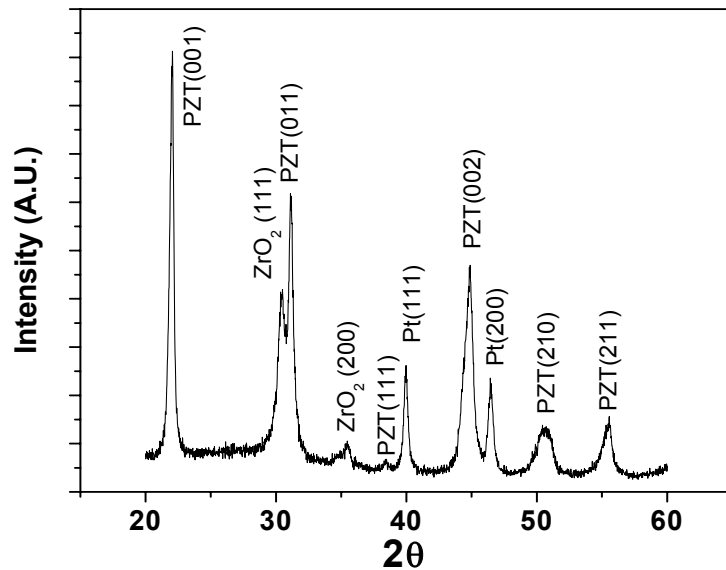
(f) Packaging & PZT poling



# Characterization of PZT films



XRD peaks of PZT film



# PZT characterization

High performance PZT thin film

$-d_{33}=200$  pC/N,  $d_{31}=-100$  pC/N,

$-\varepsilon=1200$ ,

$-\tan\delta=0.02$  at 15 kHz

# Cantilever Bow Control

Photos removed for copyright reasons.  
Source: Jeon, Y.B., R. Sood, J.H. Joeng and S.G. Kim. "Piezoelectric Micro Power Generator for Energy Harvesting." Sensors and Actuators A: Physical, accepted for publication, 2005.

ZrO<sub>2</sub>(0.05um)/  
thermal oxide(0.4um)

**(A)**

—————→  
Towards  
Tensile stress

ZrO<sub>2</sub>(0.05um)/  
PECVD oxide(0.4 um)

**(B)**

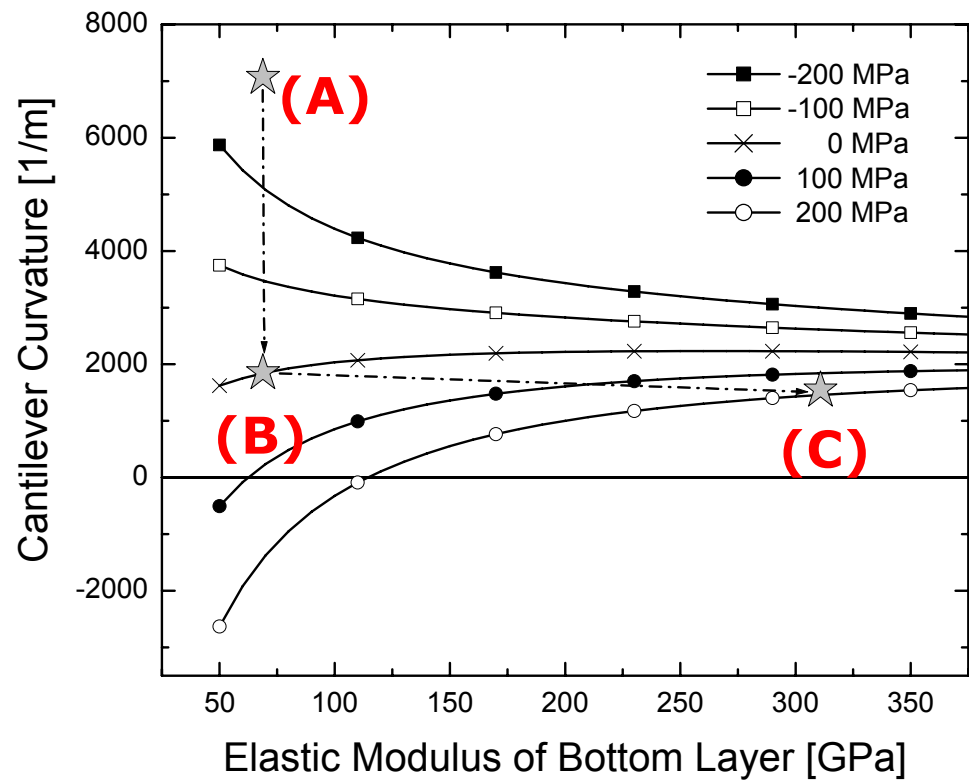
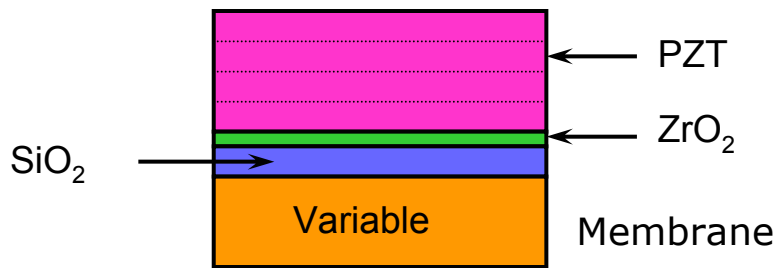
—————→  
Towards  
High elastic modulus

ZrO<sub>2</sub>(0.05um)/  
PECVD oxide(0.1um)/  
LPCVD nitride(0.4um)

**(C)**

# Cantilever Bow Control (II)

Cantilever Beam Structure



# Fabricated PMPG devices

Photos removed for copyright reasons.

Source: Jeon, Y.B., R. Sood, J.H. Joeng and S.G. Kim. "Piezoelectric Micro Power Generator for Energy Harvesting." Sensors and Actuators A: Physical, accepted for publication, 2005.

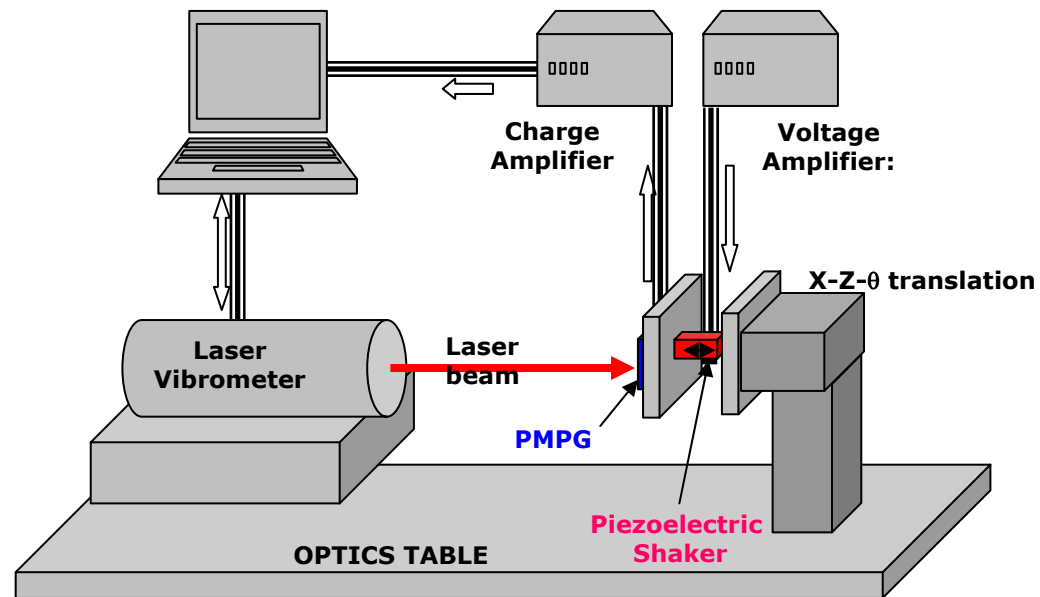
**Top view of PMPG**

**SEM image of PMPG**

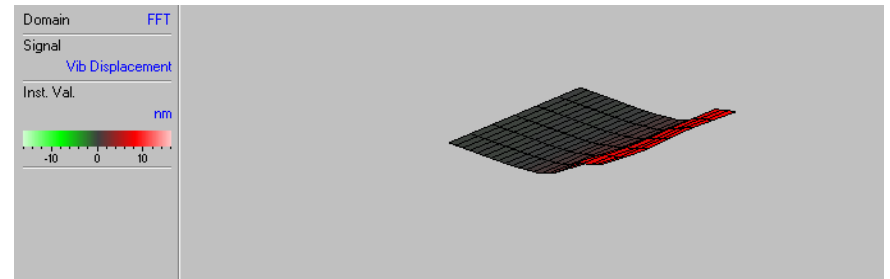
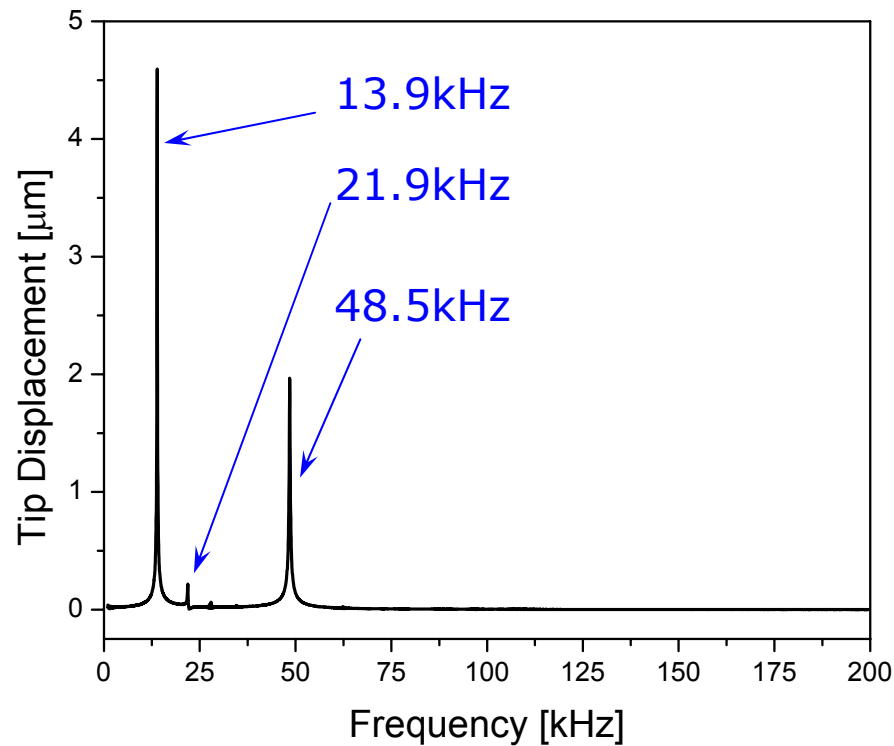
**Multiple cantilever device**

**SEM image of PMPG**

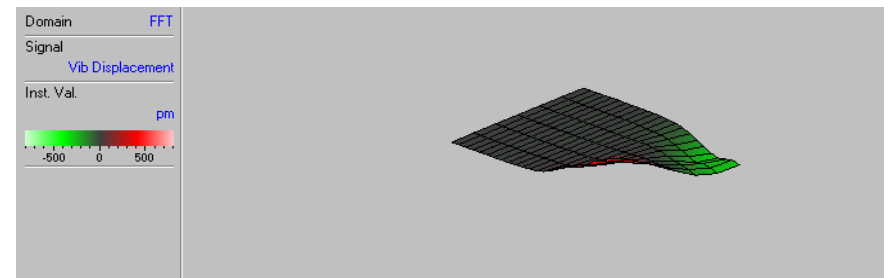
# Set-up for measurement



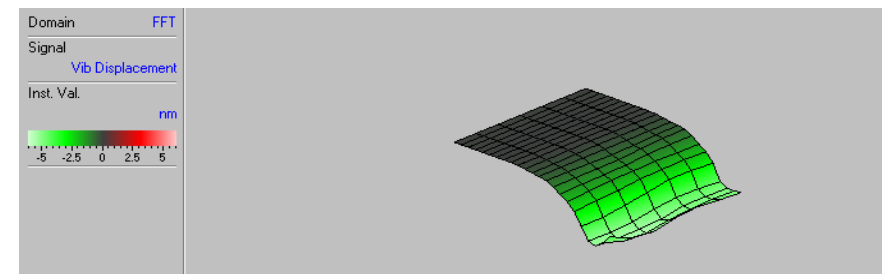
# Resonant Response of Cantilever Tip



**1<sup>st</sup> mode at 13.9 kHz**



**2<sup>nd</sup> mode at 21.9 kHz**

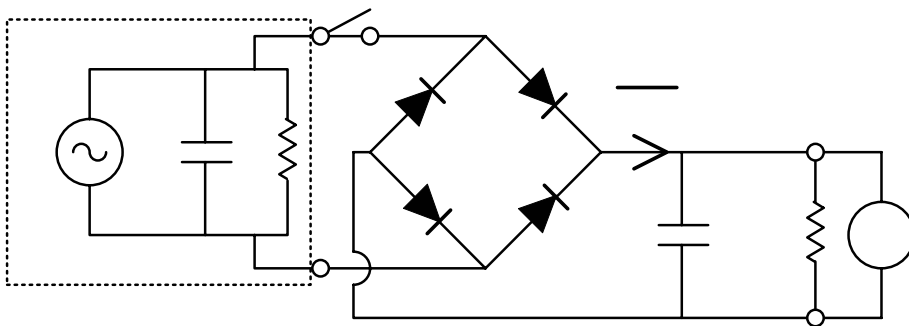


**3<sup>rd</sup> mode at 48.5 kHz**

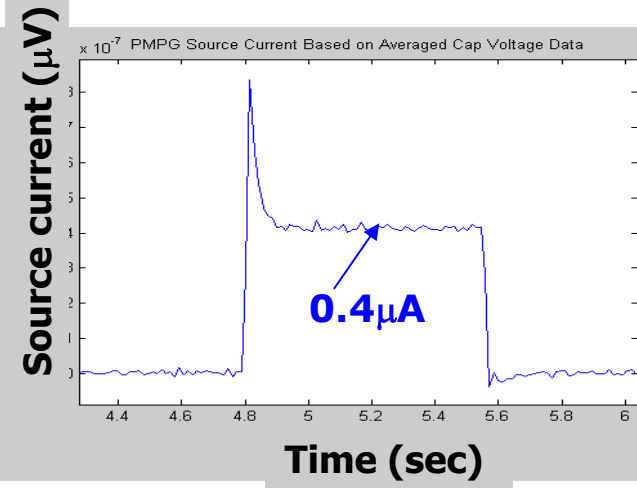
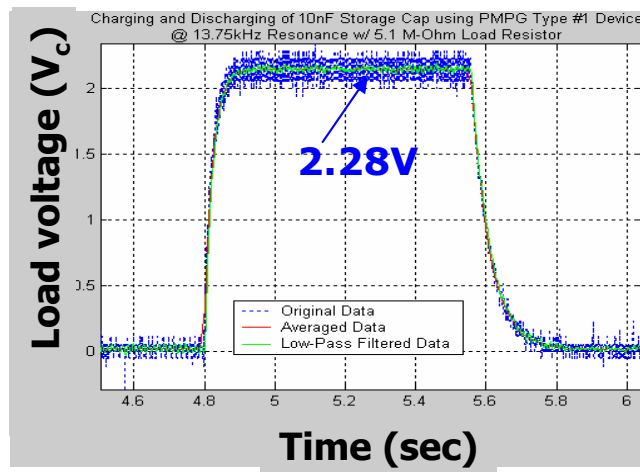


# Power Generation

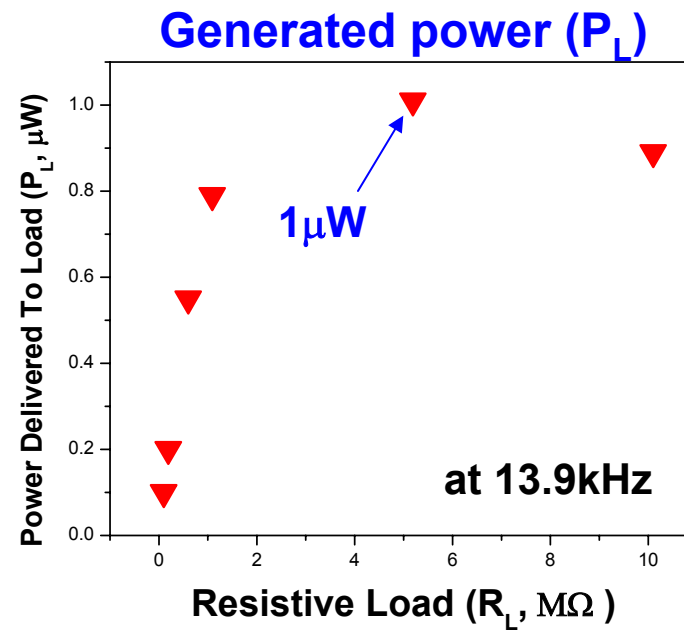
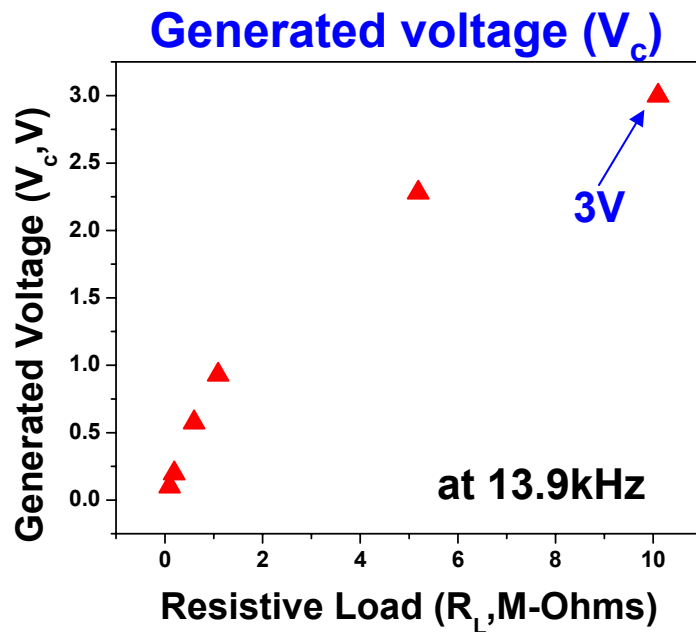
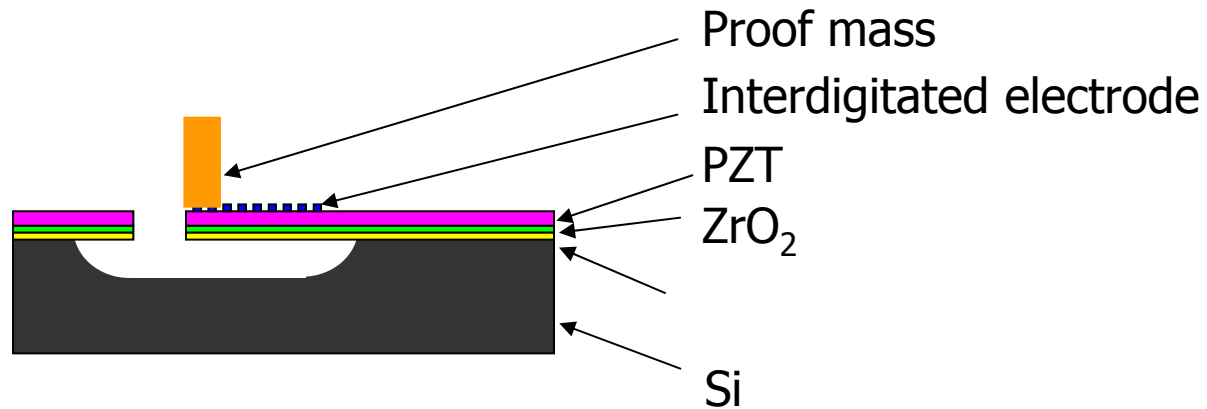
- First mode of resonance at 13.9 kHz with 14 nm amplitude
- Rectifying the AC signal, then store the charge
- Variation of load resistance



Schottky diodes: smallest forward voltage drop  
10 nF mylar cap: low leakage current



# Measurement of generated power



Y. Jeon, R. Sood, and S.G. Kim, Hilton Head Conference 2004

# Summary

Characteristic	Li/MnO <sub>2</sub>	Li/LiCoO <sub>2</sub>	PMPG
Nominal OCV	3.1 V	4 V	3V
Internal Construction	Spiral	Thin Film	MEMS Packaging
Hermeticity	Nonhermetic	Nonhermetic	Excellent
Energy Density	637 Wh/L	0.8 mWh/cm <sup>2</sup>	0.74 mWh/cm <sup>2</sup>
Operating Temperature	-20~60°C	-50~180°C	-20~80°C
Storage Conditions	10 years	60,000 cycles (charge/discharge)	Infinite

- Energy conversion efficiency ( $\eta_p$ )  
 $\eta_p = \text{generated energy}/\text{input energy}$   
 $\approx 65 \text{ to } 78 \%$
- No voltage source needed
- Open circuit voltage: 3V

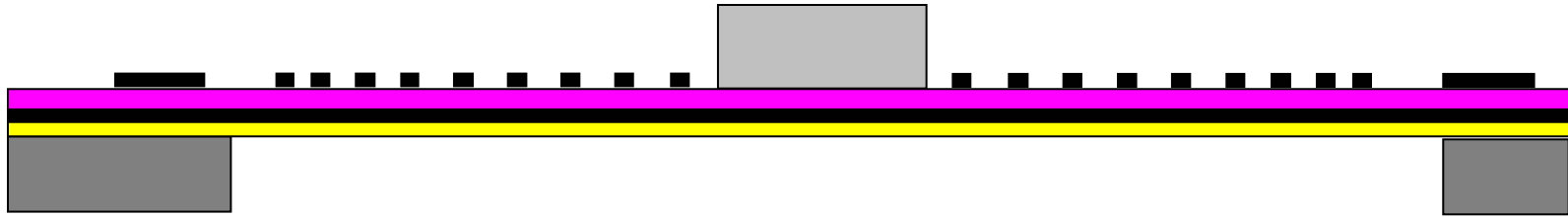
## ***Power depends on***

- Resonant Frequency
  - Internal Capacitance and Resistance
  - External Capacitance and Load Resistance
  - Mechanical damping
  - Membrane structure
  - Electrode shape
- 
- Bow control?
  - Multi-cantilever → Multiple bridges?



**New Design for  
Efficient Power Harvesting**

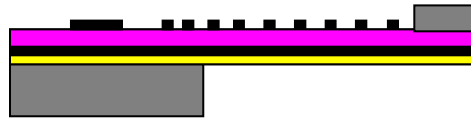
## In progress,



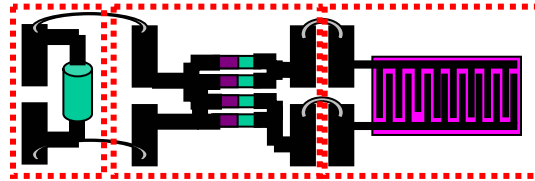
- High resonant frequency products
  - Bridge Structures vs. Cantilevers
  - Smart bearings
- Low resonant frequency structures
  - Scavengers
- Monolithic Device Design
  - Mechanical Rectifiers

# Self-supportive Wireless Sensors

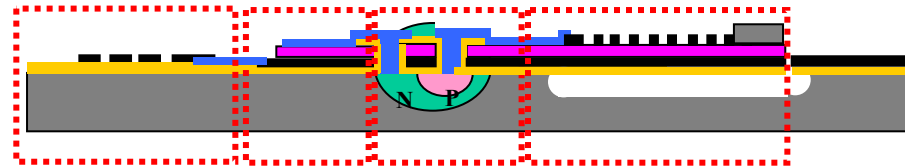
Design and fabrication



Concept prove



New Design & PMPG integration



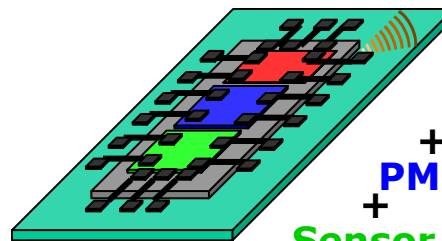
RF circuit

Storage

Rectifier

Generator

On chip RFID  
with PMPG and Sensor

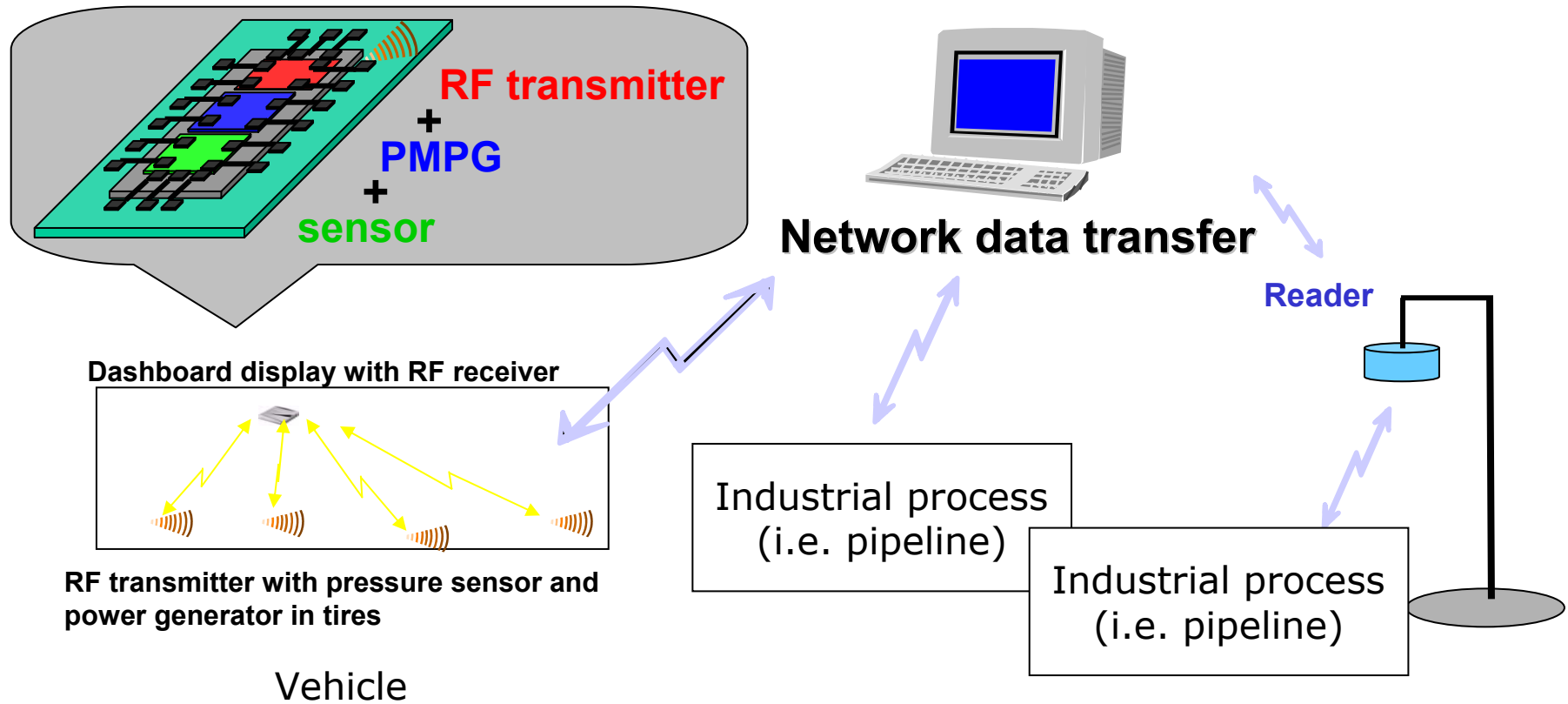


RF transmitter

+  
PMPG

+  
Sensor

# Wireless Sensing Applications



## Self-supportive Sensors

# Can we avoid disasters?

## Belgian gas pipe blast kills 15, destroys plants

Photo removed for copyright reasons

GHISLENGHIEN (Belgium) July 30 - A huge blast on a leaking gas pipeline in Belgium on Friday sent giant fireballs in the air and catapulted bodies hundreds of metres in the biggest industrial disaster in the country's recent history.

At least 15 people were killed and more than 100 injured when the explosion ripped through the underground pipeline in the industrial zone of Ghislenghien, near the town of Ath, 40 km (25 miles) southwest of Brussels.

**PICTURE shows the cut gas pipeline which exploded at an industrial estate in Ghislenghien, southern Belgium, July 30. - AFPpix.**