

13.024

Spring 2003

Homepleasure 2

(Because, really, we're all delighted to learn yet another programming language...)

Due Tuesday, February 25

**Exercise 1 Vectorizing your code.** Without using any loops (or typing the elements in), use the following vector:

$$\mathbf{x} = [1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \ 10]$$

to construct the following matrix (note the pattern in the values of each row and column).

$$\begin{bmatrix} 1 + 10i & 2 + 9i & 3 + 8i & 4 + 7i & 5 + 6i & 6 + 5i & 7 + 4i & 8 + 3i & 9 + 2i & 10 + i \\ 2 + 9i & 3 + 8i & 4 + 7i & 5 + 6i & 6 + 5i & 7 + 4i & 8 + 3i & 9 + 2i & 10 + i & 1 + 10i \\ 3 + 8i & 4 + 7i & 5 + 6i & 6 + 5i & 7 + 4i & 8 + 3i & 9 + 2i & 10 + i & 1 + 10i & 2 + 9i \\ 4 + 7i & 5 + 6i & 6 + 5i & 7 + 4i & 8 + 3i & 9 + 2i & 10 + i & 1 + 10i & 2 + 9i & 3 + 8i \\ 5 + 6i & 6 + 5i & 7 + 4i & 8 + 3i & 9 + 2i & 10 + i & 1 + 10i & 2 + 9i & 3 + 8i & 4 + 7i \\ 6 + 5i & 7 + 4i & 8 + 3i & 9 + 2i & 10 + i & 1 + 10i & 2 + 9i & 3 + 8i & 4 + 7i & 5 + 6i \\ 7 + 4i & 8 + 3i & 9 + 2i & 10 + i & 1 + 10i & 2 + 9i & 3 + 8i & 4 + 7i & 5 + 6i & 6 + 5i \\ 8 + 3i & 9 + 2i & 10 + i & 1 + 10i & 2 + 9i & 3 + 8i & 4 + 7i & 5 + 6i & 6 + 5i & 7 + 4i \\ 9 + 2i & 10 + i & 1 + 10i & 2 + 9i & 3 + 8i & 4 + 7i & 5 + 6i & 6 + 5i & 7 + 4i & 8 + 3i \\ 10 + i & 1 + 10i & 2 + 9i & 3 + 8i & 4 + 7i & 5 + 6i & 6 + 5i & 7 + 4i & 8 + 3i & 9 + 2i \end{bmatrix}$$

**Exercise 2 Matrix element manipulation** Write an m-file. Within this file, create 3 matrices

$$A = \begin{bmatrix} 1 + i & 2 - i & 3 - i \\ 4 & 5 & 6 - i \\ 7 - i & 8 - i & 9 + i \end{bmatrix} \quad B = \begin{bmatrix} 1 + i & 2 - 2i \\ 5 & 6 - i \\ 11i & 9 + i \end{bmatrix} \quad C = \begin{bmatrix} 1 \\ 6 - i \\ 6 \end{bmatrix}$$

Within this file, use Matlab's commands to find their transposes,  $A^T, B^T, C^T$  and to find the elements with the largest absolute values in each row of these

transposes. Find the inverse of  $A$ . Using Matlab commands, locate all elements of  $A^{-1}$  with absolute value greater than 3 and less than 7. Output both these values and their indices as would appear in matrix notation. For example, if

$$A^{-1} = \begin{bmatrix} 1 & 2 \\ 4 & 6 \end{bmatrix}$$

then  $A_{12}^{-1} = 2$  and  $A_{22}^{-1} = 6$  would satisfy this condition. The indices for these elements would then be 12 and 22 or equivalently  $m = 1, n = 2$  and  $m = 2, n = 2$ .

**Exercise 3 Writing functions** In an m-file, write a *function* named `logm2` which will calculate the base ten logarithm of every value of an input vector and subtract two from it. The function should return this new vector with the variable name `lv2`.

**Exercises 4-7 Pulling it all together** Write a modular m-file program with the following parts: the main program calling 3 subprograms, a subprogram which reads data files and manipulates this data, a subprogram which plots data and a subprogram which outputs data. Comment each of these files appropriately.

4 The first data file will be a `.mat` file which you will need to create. Put these values into it:

$$x = 1 : .43 : 68; \quad y = \log_2(x);$$

using the `save` command.

The second data file will be an `ascii` file which you will find in my public directory. To copy a file from my public directory to your athena directory, you can either type

```
cp /afs/athena.mit.edu/user/b/r/browns/Public/hmpl2 hmpl2
```

at an Athena prompt, or you can copy it using your favorite web browser at

<http://web.mit.edu/browns/Public/>

The first subprogram should read the two data files - as they are different types of files, different methods of reading them will need to be employed. The `.mat` file can be read using the `load` command. The `ascii` file will need to be read using a combination of `fopen`, `fscanf` or `fgetl`, and `fclose`.

Once the variables, `x`, `y`, `z` have been read in from their respective data files, the function `logm2` which you made in exercise 3 should be applied to each of them. You will now have 3 new variables which comprise

$$xl2 = \log_{10}(x) - 2 \quad yl2 = \log_{10}(y) - 2 \quad zl2 = \log_{10}(z) - 2$$

5 The second subprogram should contain plotting commands. You are asked to plot  $xl2$  v.  $yl2$ ,  $yl2$  v.  $zl2$  and  $xl2$  v.  $zl2$  in three log-log subplots in a single figure. Each plot should have appropriately labeled axes, a title, and a legend. Plot both the data pairs (points) and a line connecting them. The figure number should be specified and each subplot should be cleared before plotting each time the program is run.

6 The third subprogram should output the new variables into two different files. The first file should be a .mat file and the second an ascii file. The .mat file can be made using the *save* command. In the ascii file, each variable should be saved in exponential form and separated by 4 spaces using *fopen*, *fprintf* and *fclose*.

7 The main program should look something like

```
% main program
```

```
subprogram1  
subprogram2  
subprogram3
```

with whatever set of program names you like.

The main program and subprograms should be mailed to [browns@mit.edu](mailto:browns@mit.edu). They can be either in .m format from your Matlab editor, or text files. No emacs, MSword, or other word processor files please. Please send each program as a separate attachment and include your name or nickname within the name of the main program. A printout of all programs for the exercises and results should be handed in as well.