

Thermodynamics of Materials

3.00 Fall 2002

Problem Set 6

Exercise 6.1

Methane CH_4 and carbon dioxide CO_2 are mixed in equal molar proportions in a reservoir fixed at $T = 1750\text{K}$ and 1 atmosphere pressure. Find the equilibrium concentrations of the gaseous components.

Assume that the only gaseous components are CH_4 , CO_2 , H_2 , CO , O_2 , and H_2O .

Free energies as a function of temperature for several reactions are tabulated below:

Reaction	Change in Molar Gibbs Free Energy (joules)
$\text{CH}_4(\text{gas}) \rightleftharpoons \text{C}(\text{graphite}) + 2\text{H}_2(\text{gas})$	$69120 - 22.25T \log T + 65.35T$
$2\text{CO}(\text{gas}) \rightleftharpoons 2\text{C}(\text{graphite}) + \text{O}_2(\text{gas})$	$223400 + 175.3T$
$\text{CO}_2(\text{gas}) \rightleftharpoons \text{C}(\text{graphite}) + \text{O}_2(\text{gas})$	$394100 + 0.8T$
$\text{H}_2(\text{gas}) + \frac{1}{2}\text{O}_2(\text{gas}) \rightleftharpoons \text{H}_2\text{O}(\text{gas})$	$-246400 + 54.8T$

Exercise 6.2

Find an expression that relates the change in Gibbs free energy with temperature at constant volume, $(\frac{\partial G}{\partial T})_V$, in terms of the, entropy, volume, thermal expansivity $\alpha \equiv \frac{1}{V} (\frac{\partial V}{\partial T})_P$, and the isothermal compressibility $\kappa_T \equiv -\frac{1}{V} (\frac{\partial V}{\partial P})_T$.

Describe how you would measure κ_T and α in an experiment.